

# Engineering Software

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# Power Cycles Analysis with Plots

In this power cycles analysis, the engineering students and professionals get familiar with the ideal simple and basic power cycles and their T - s, p - V and h - T diagrams, operation and major performance trends when air is considered as the working fluid.

Performance Objectives:

Introduce basic energy conversion engineering assumptions and equations

Know basic elements of Carnot Cycle, Brayton Cycle, Otto Cycle and Diesel Cycle and their T - s, p - V and h - T diagrams

Be familiar with Carnot Cycle, Brayton Cycle, Otto Cycle and Diesel Cycle operation

Understand general Carnot Cycle, Brayton Cycle, Otto Cycle and Diesel Cycle performance trends

# Engineering Assumptions

The power cycles analysis presented in this material considers ideal (isentropic) operation and the working fluid is air. Furthermore, the following assumptions are valid:

## **Power Cycles**

Single species consideration -- fuel mass flow rate is ignored and its impact on the properties of the working fluid

Basic equations hold (continuity, momentum and energy equations)

Specific heat is constant

## **Power Cycle Components/Processes**

Single species consideration

Basic equations hold (continuity, momentum and energy equations)

Specific heat is constant

# Basic Engineering Equations

## Basic Conservation Equations

Continuity Equation

$$m = \rho v A \text{ [kg/s]}$$

Momentum Equation

$$F = (vm + pA)_{\text{out} - \text{in}} \text{ [N]}$$

Energy Equation

$$Q - W = ((h + v^2/2 + gh)m)_{\text{out} - \text{in}} \text{ [kW]}$$

# Basic Engineering Equations

Ideal Gas State Equation

$$pv = RT \text{ [kJ/kg]}$$

Perfect Gas

$$c_p = \text{constant [kJ/kg}^{\circ}\text{K]}$$

Kappa

$$\chi = c_p/c_v \text{ []}$$

For air:  $\chi = 1.4 \text{ []}$ ,  $R = 0.2867 \text{ [kJ/kg}^{\circ}\text{K]}$  and

$$c_p = 1.004 \text{ [kJ/kg}^{\circ}\text{K]}$$

# Power Cycles Engineering Equations

Cycle Efficiency

$$\eta = W_{\text{net}}/Q \text{ [/]}$$

Heat Rate

$$\text{HR} = (1/\eta)3,412 \text{ [Btu/kWh]}$$

Carnot Cycle Efficiency

$$\eta = 1 - T_R/T_A$$

Brayton Cycle Efficiency

$$\eta = 1 - 1/r_p^{(X-1)/X}$$

Otto Cycle Efficiency

$$\eta = 1 - 1/\varepsilon^{(X-1)}$$

Diesel Cycle Efficiency

$$\eta = 1 - (\phi^{X-1}) / (X\varepsilon^{(X-1)}(\phi-1))$$

$$r_p = p_2/p_1 \text{ [/]}; \varepsilon = V_1/V_2 \text{ [/]}; \phi = V_3/V_2 \text{ [/]}$$

# Power Cycles Engineering Equations

## Brayton Cycle

$$w_{\text{net}} = q_h - q_l = c_p(T_3 - T_2) - c_p(T_4 - T_1) \text{ [kJ/kg]}$$
$$W_{\text{net}} = w_{\text{net}} m \text{ [kW]}$$

## Otto Cycle

$$w_{\text{net}} = q_h - q_l = c_v(T_3 - T_2) - c_v(T_4 - T_1) \text{ [kJ/kg]}$$
$$W_{\text{net}} = w_{\text{net}} m \text{ [kW]}$$

## Diesel Cycle

$$w_{\text{net}} = q_h - q_l = c_p(T_3 - T_2) - c_v(T_4 - T_1) \text{ [kJ/kg]}$$
$$W_{\text{net}} = w_{\text{net}} m \text{ [kW]}$$

# Power Cycle Components/Processes

## Engineering Equations

Isentropic Compression

$$T_2/T_1 = (p_2/p_1)^{(X-1)/X} \text{ [/]}$$

$$T_2/T_1 = (V_1/V_2)^{(X-1)} \text{ [/]}$$

$$p_2/p_1 = (V_1/V_2)^X \text{ [/]}$$

$$w_c = c_p(T_2 - T_1) \text{ [kJ/kg]}$$

$$W_c = c_p(T_2 - T_1)m \text{ [kW]}$$



# Power Cycle Components/Processes

## Engineering Equations

Isentropic Expansion

$$T_1/T_2 = (p_1/p_2)^{(X-1)/X} \text{ [/]}$$

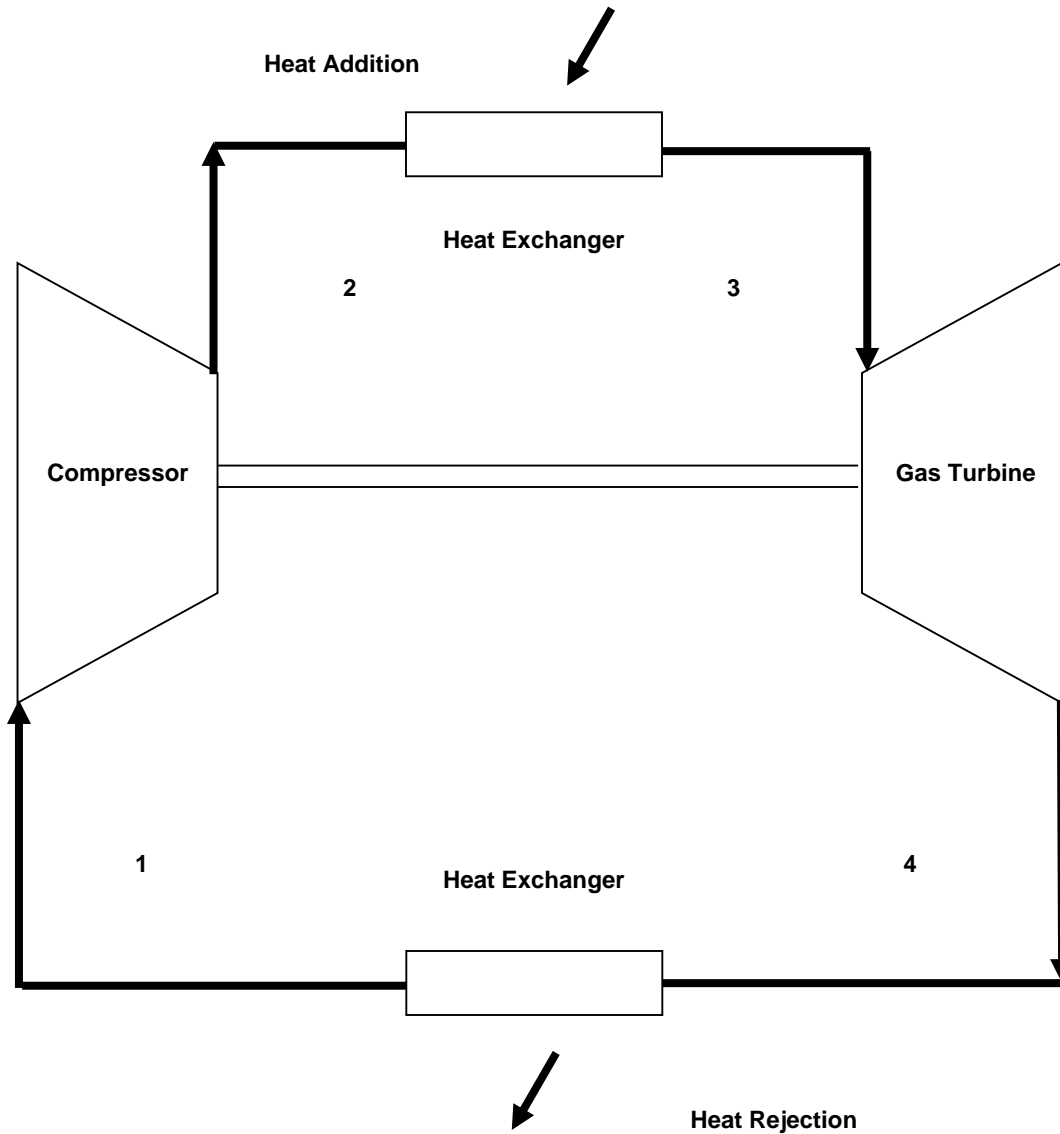
$$T_1/T_2 = (V_2/V_1)^{(X-1)} \text{ [/]}$$

$$p_1/p_2 = (V_2/V_1)^X \text{ [/]}$$

$$w_e = c_p(T_1 - T_2) \text{ [kJ/kg]}$$

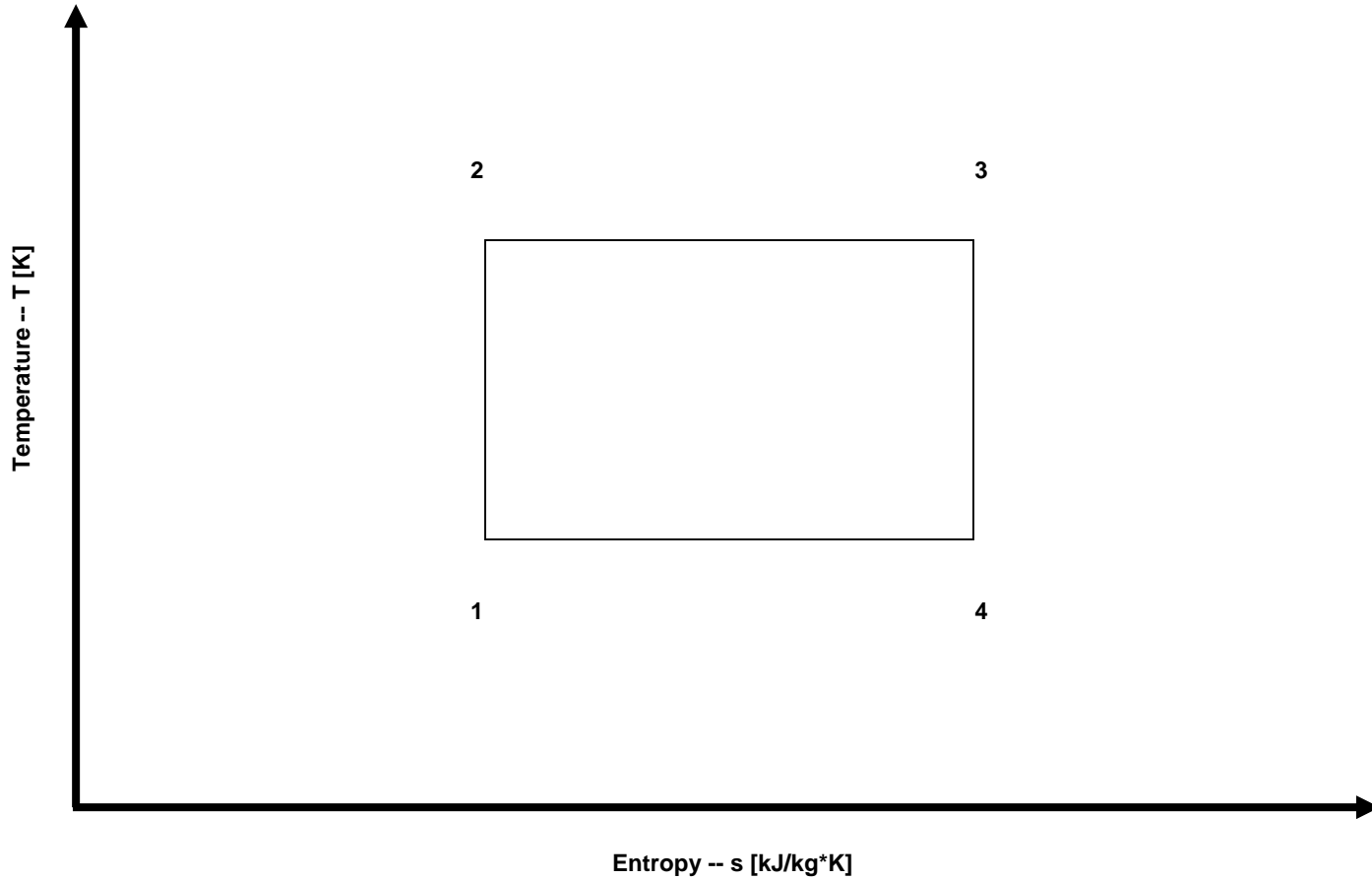
$$W_e = c_p(T_1 - T_2)m \text{ [kW]}$$

# Carnot Cycle



Carnot Cycle Schematic Layout

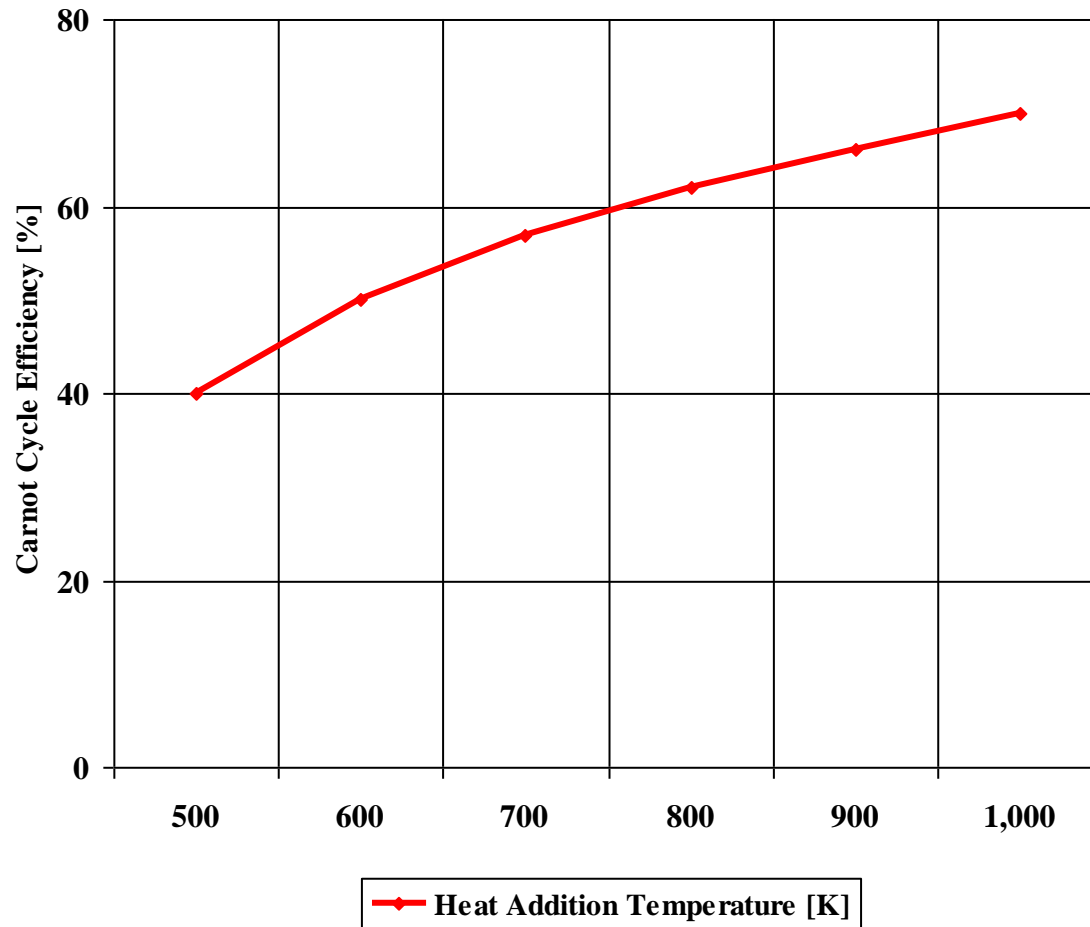
# Carnot Cycle



Carnot Cycle T - s Diagram

# Carnot Cycle

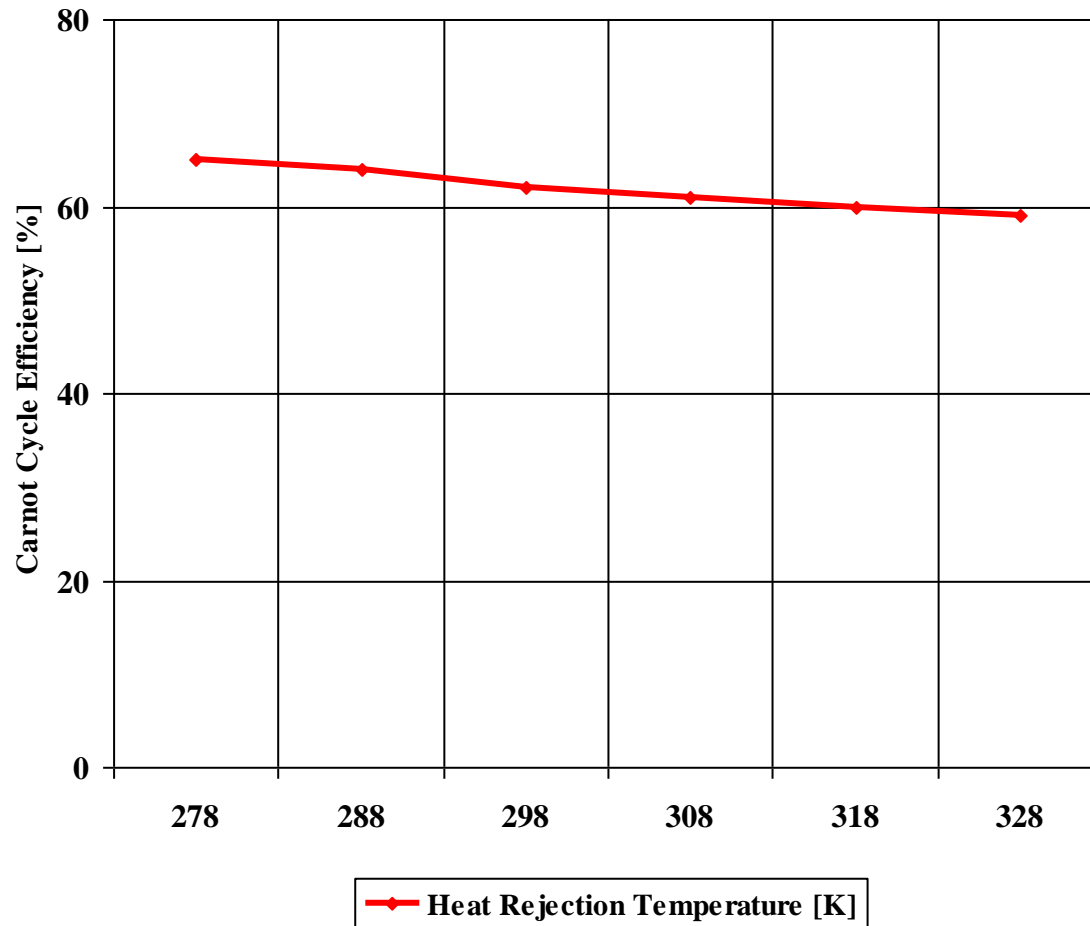
## Carnot Cycle Efficiency



Compressor Inlet Temperature: 298 [K]

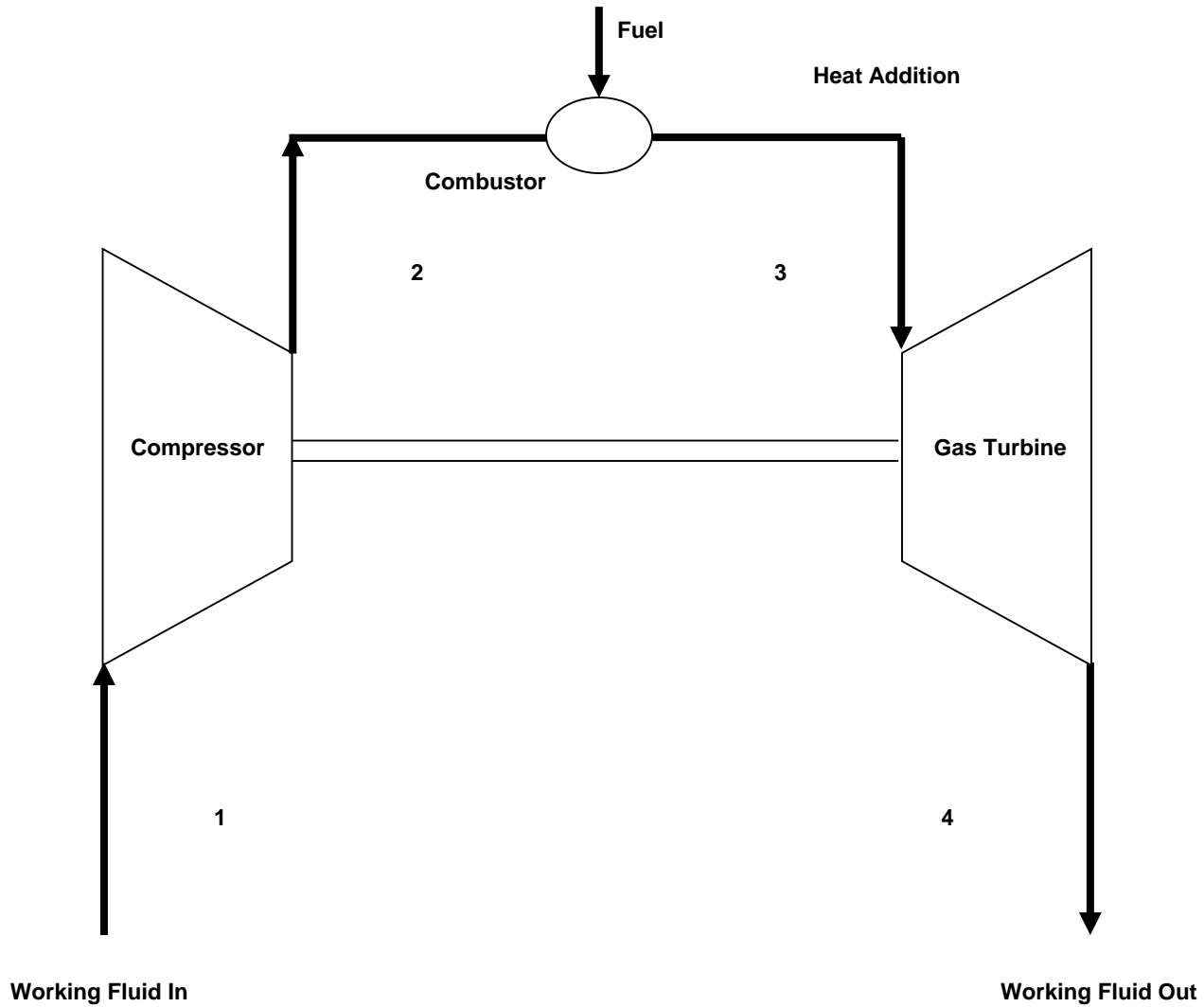
# Carnot Cycle

## Carnot Cycle Efficiency



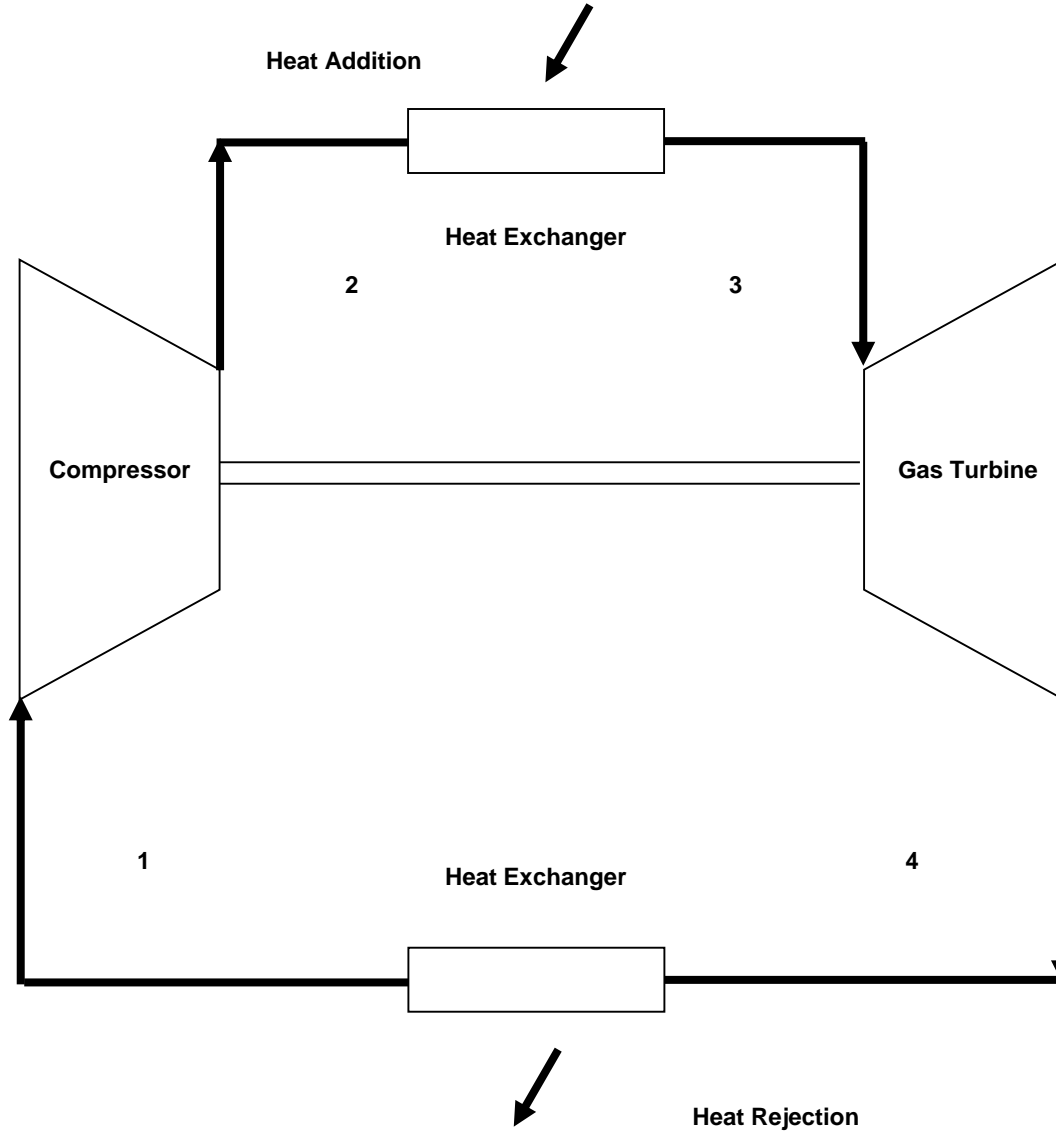
Turbine Inlet Temperature: 800 [K]

# Brayton Cycle (Gas Turbine)



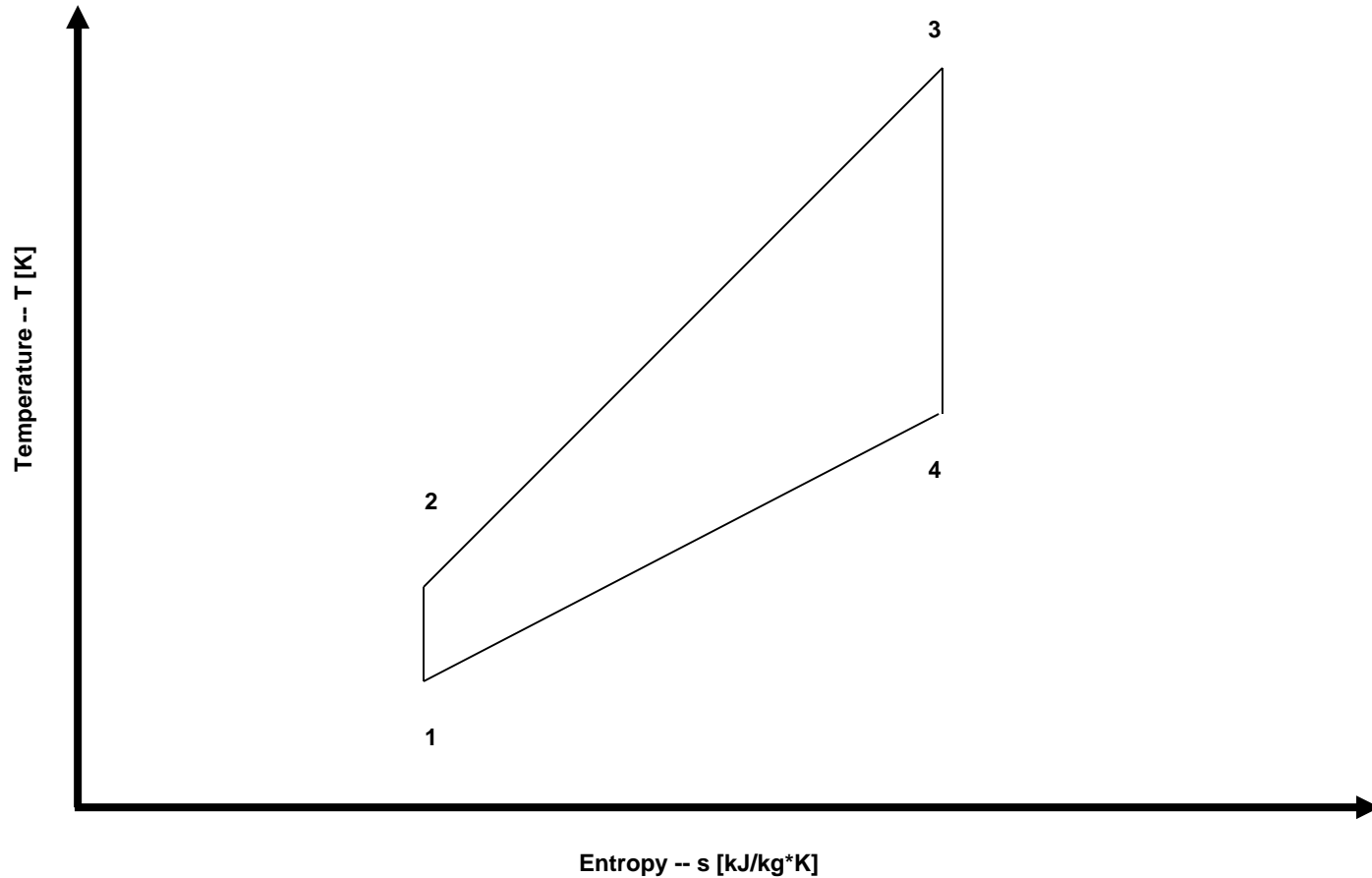
Brayton Cycle (Gas Turbine) Schematic Layout -- Open Cycle

# Brayton Cycle (Gas Turbine)



Brayton Cycle Schematic Layout -- Closed Cycle

# Brayton Cycle (Gas Turbine)



Brayton Cycle (Gas Turbine) T - s Diagram



# Brayton Cycle (Gas Turbine)

## Assumptions

Compressor Inlet Temperature: 298 [K]

Compressor Inlet Pressure: 1 [atm]

Turbine Inlet Temperature: 1,500 [K]

Turbine Inlet Pressure: 15 [atm]

Working Fluid  $\gamma$  : 1.4 [/]

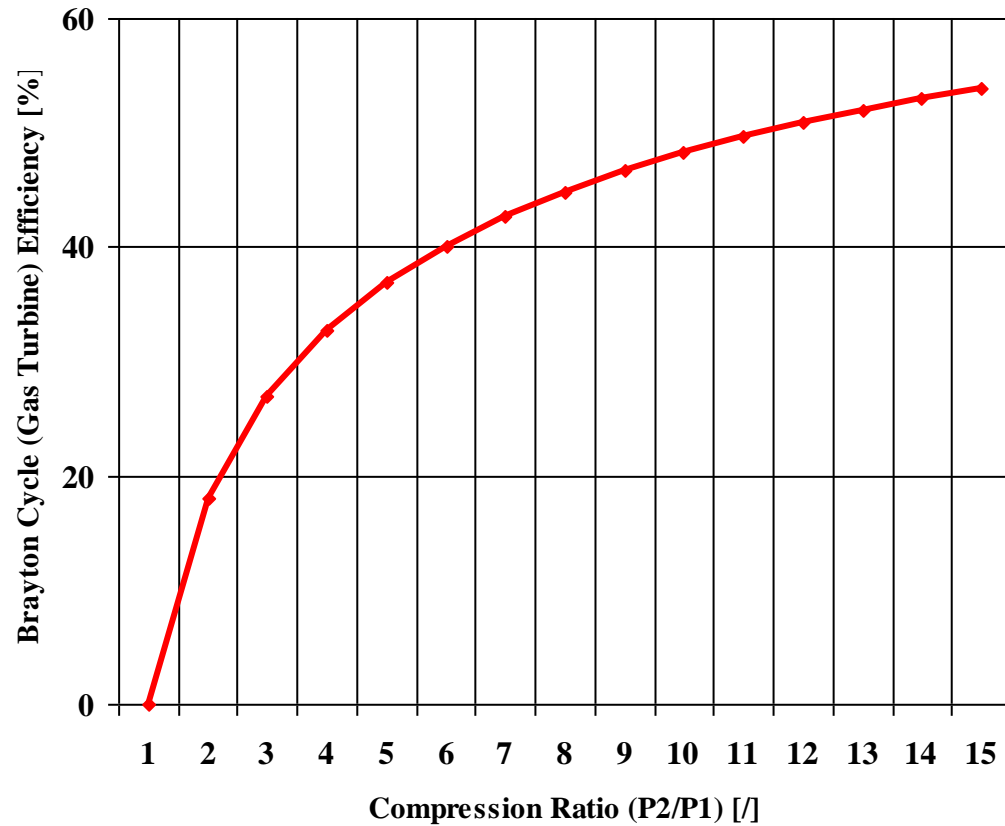
Working Fluid Specific Heat: 1.004 [kJ/kg\*K]

Working Fluid Mass Flow Rate: 1 [kg/s]

Fuel HHV: 24,000 [Btu/lbm]

# Brayton Cycle (Gas Turbine)

Brayton Cycle (Gas Turbine) Efficiency

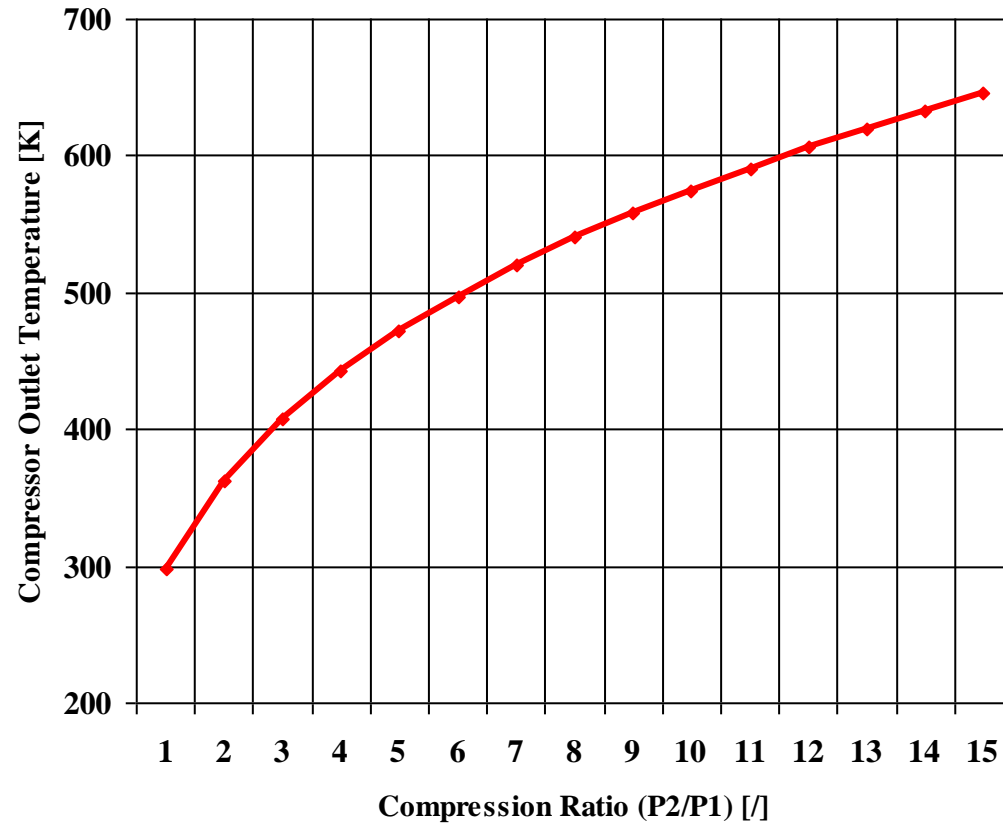


—◆— P2/P1 [ / ]

Working Fluid: Air

# Brayton Cycle (Gas Turbine)

## Compressor Outlet Temperature

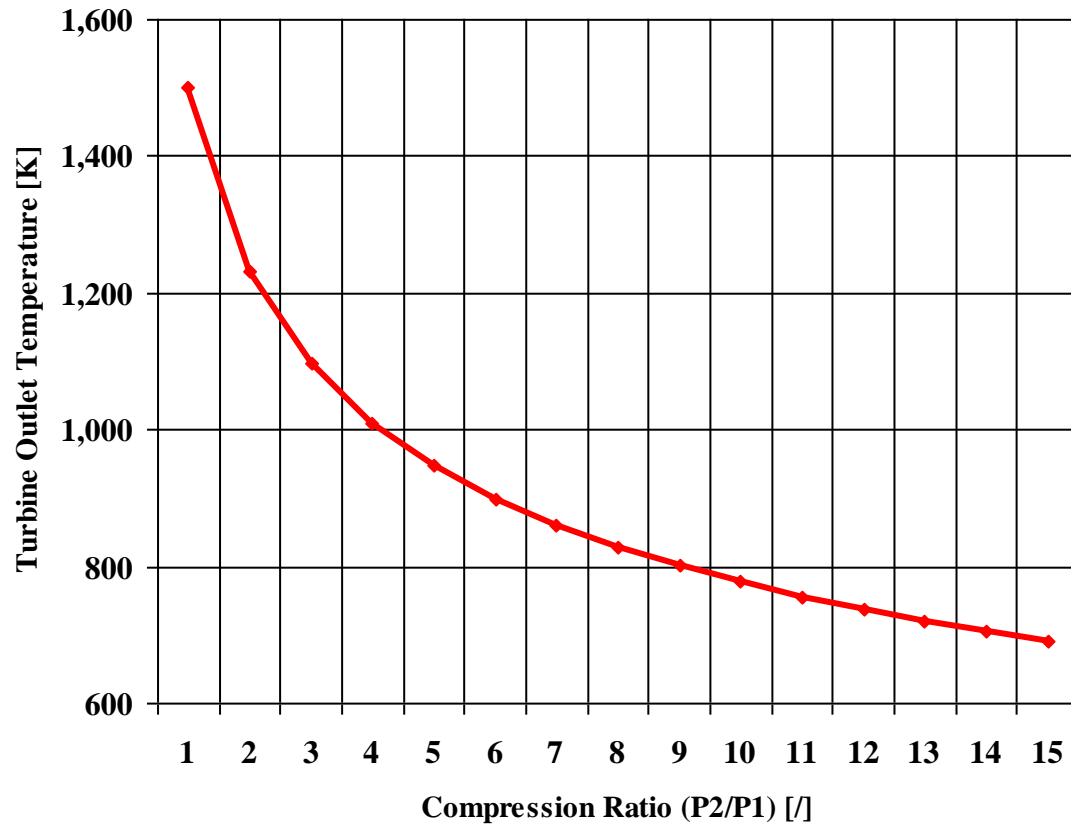


—◆— P2/P1 [ / ]

Working Fluid: Air

# Brayton Cycle (Gas Turbine)

## Turbine Outlet Temperature

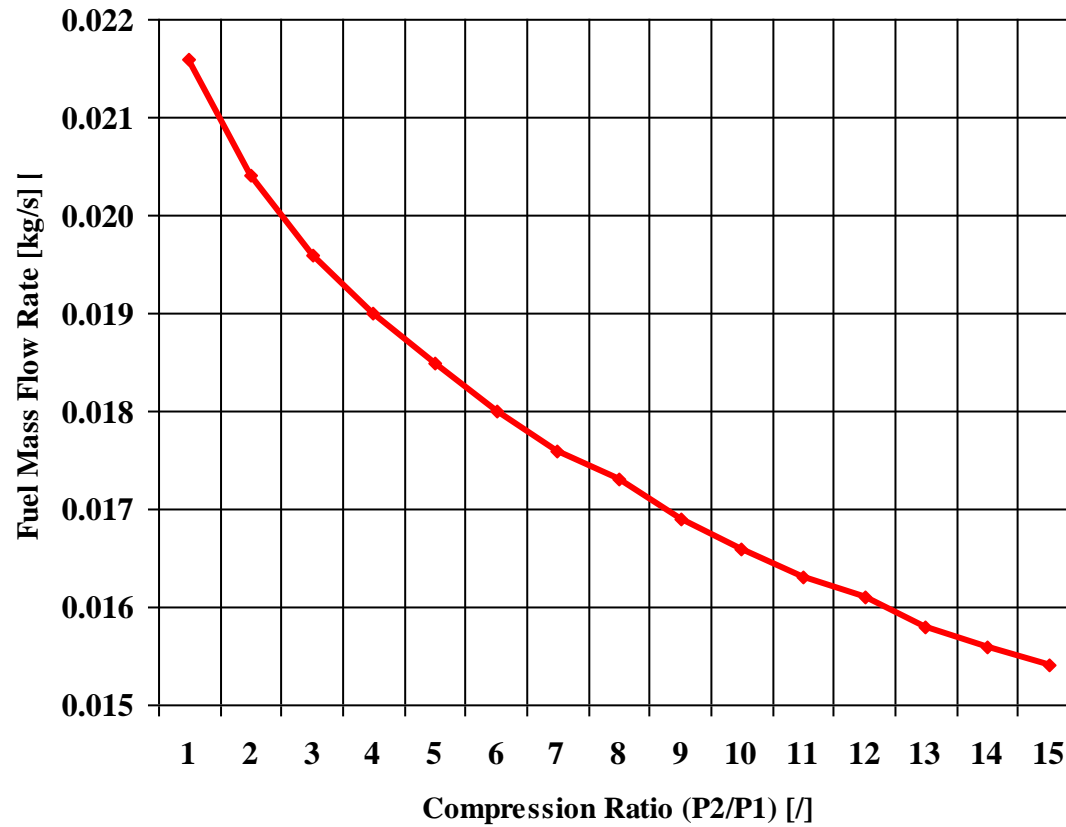


—◆— P2/P1 [1]

Working Fluid: Air

# Brayton Cycle (Gas Turbine)

Fuel Mass Flow Rate

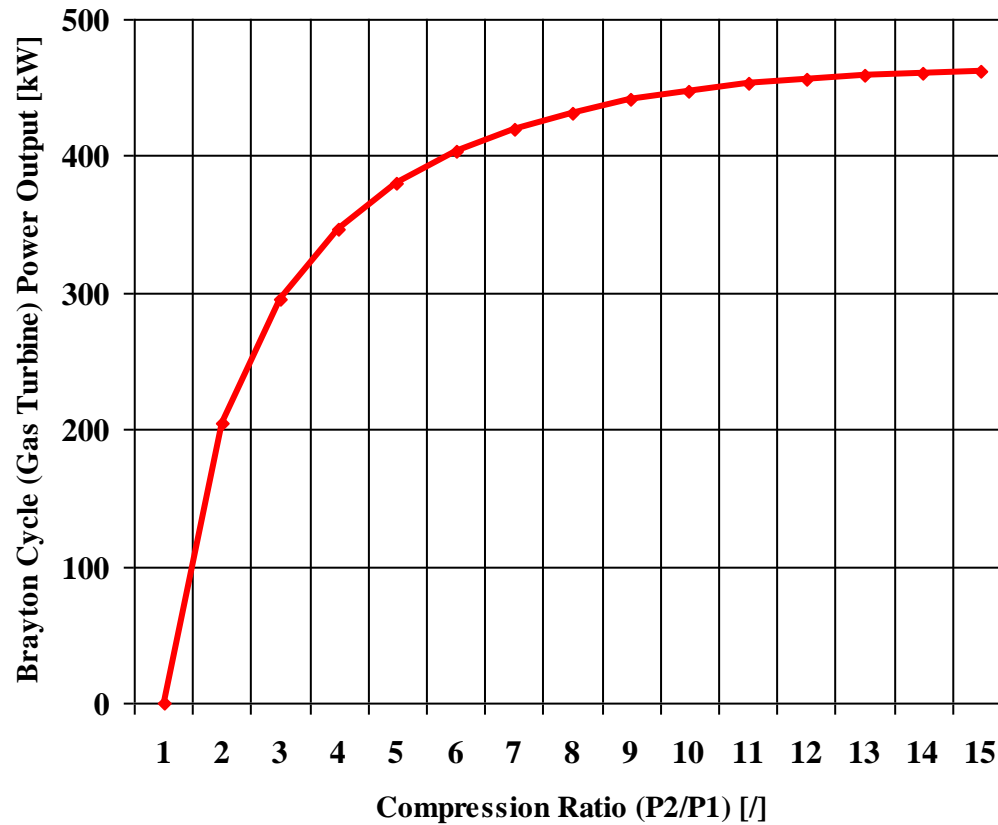


—◆— P2/P1 [ ]

Working Fluid: Air

# Brayton Cycle (Gas Turbine)

## Brayton Cycle (Gas Turbine) Power Output

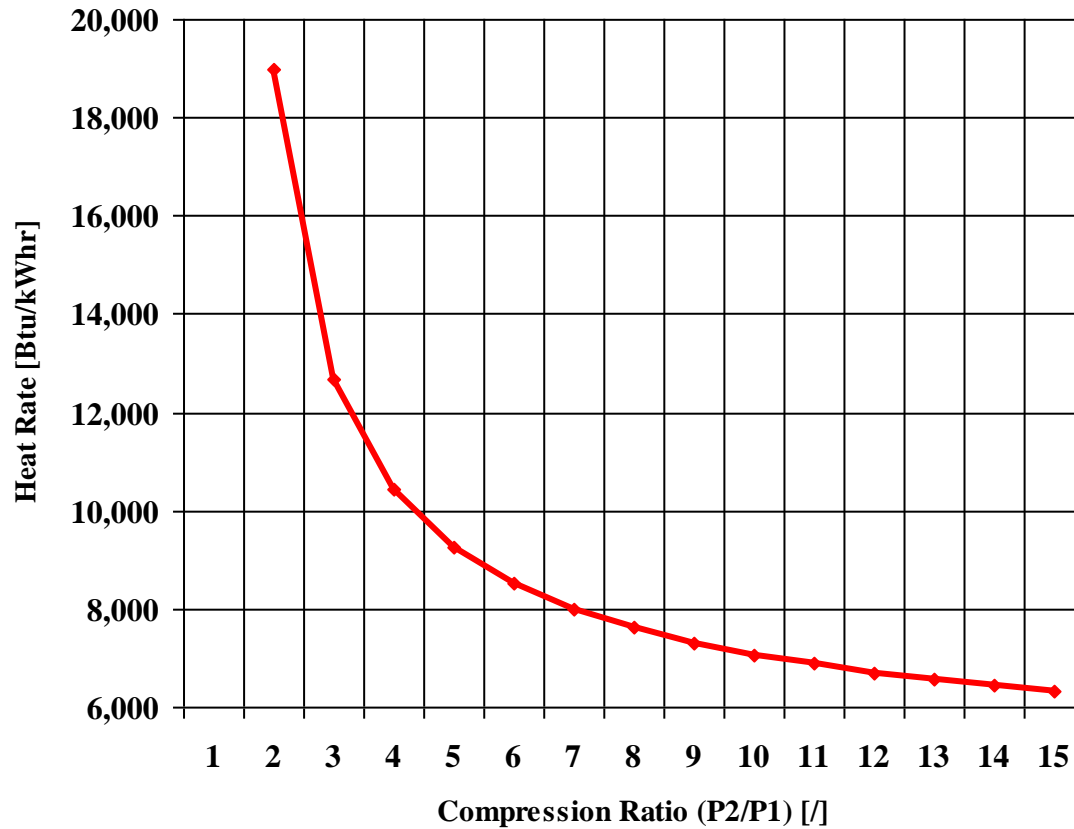


—◆— P2/P1 [1]

Working Fluid: Air

# Brayton Cycle (Gas Turbine)

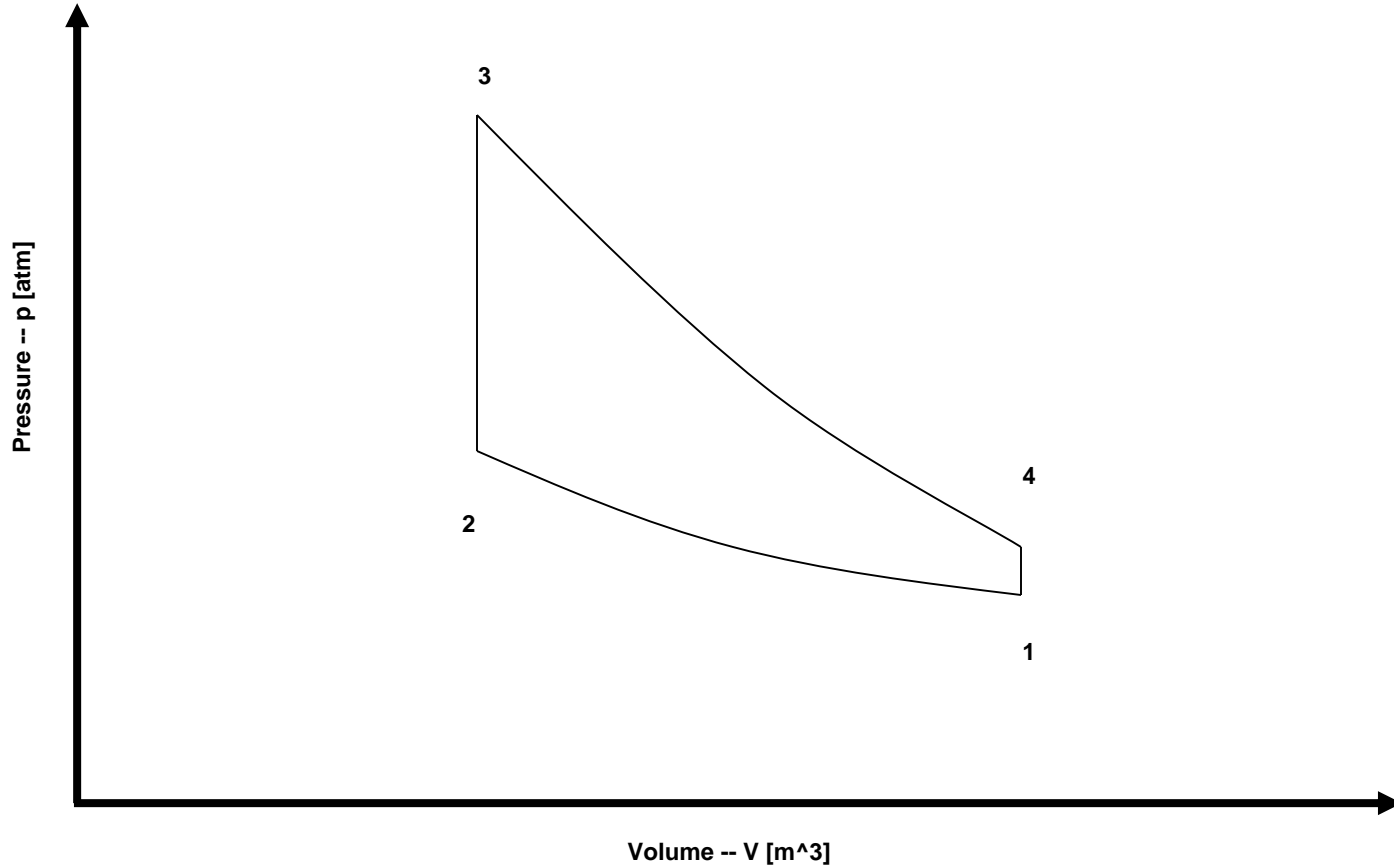
## Heat Rate



—◆— P2/P1 [ / ]

Working Fluid: Air

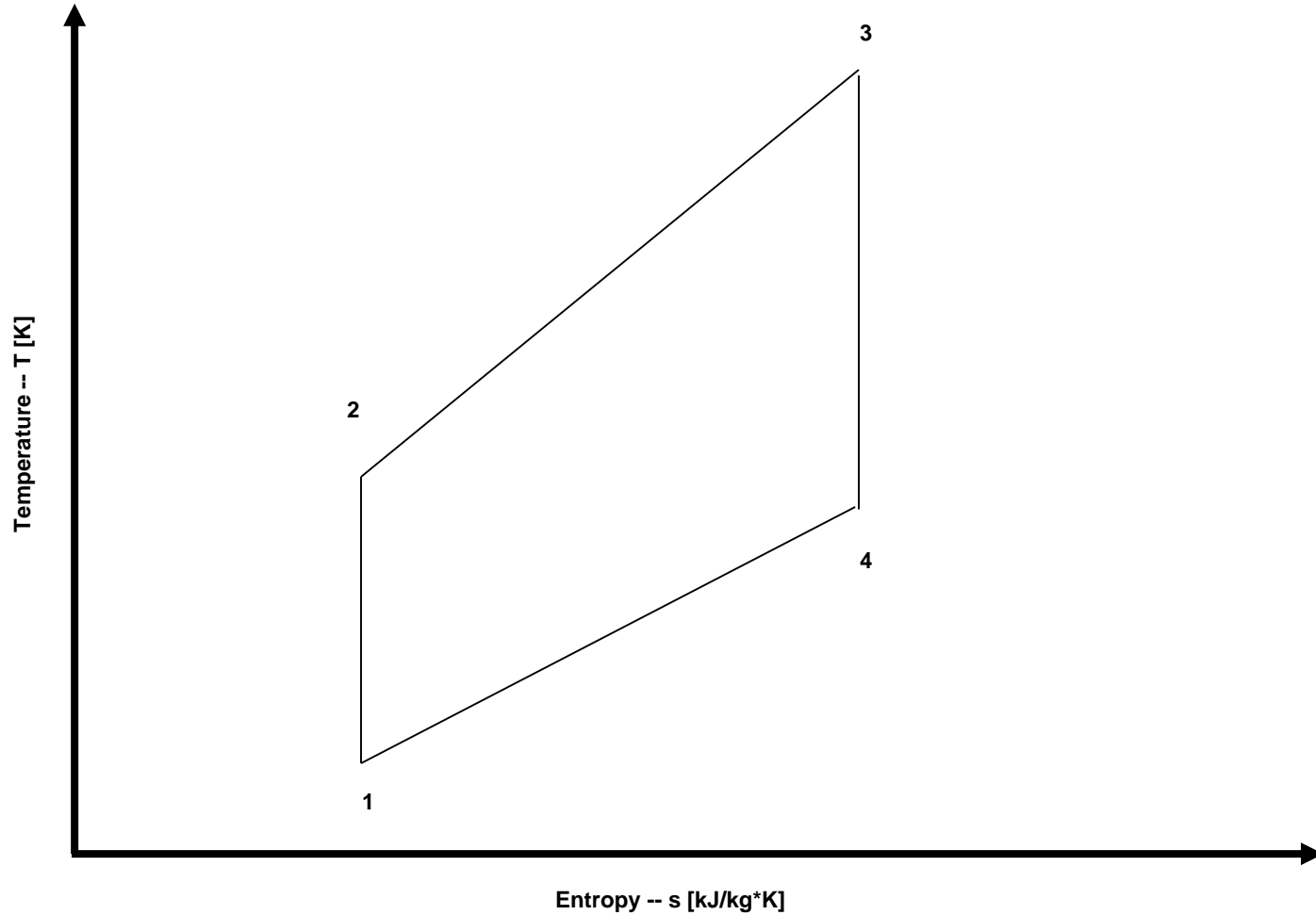
# Otto Cycle



Otto Cycle p - V Diagram



# Otto Cycle



Otto Cycle T - s Diagram

# Otto Cycle

## Assumptions

Ambient Temperature: 298 [K]

Ambient Pressure: 1 [atm]

Compression Ratio: 7 [/]

Combustion Temperature: 1,250 [K]

Working Fluid  $\gamma$  : 1.4 [/]

Working Fluid Gas Constant: 0.2867 [kJ/kg\*K]

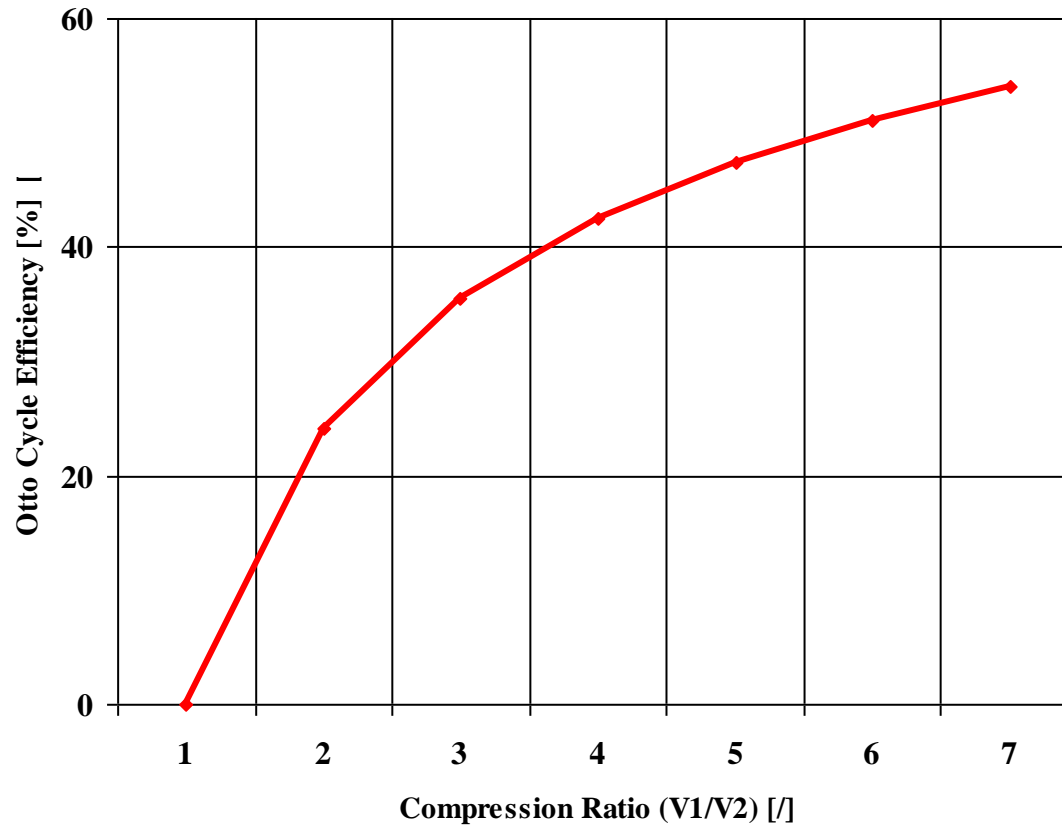
Working Fluid Specific Heat: 1.004 [kJ/kg\*K]

Working Fluid Mass Flow Rate: 0.78 [kg/s]

Fuel HHV: 18,000 [Btu/lbm]

# Otto Cycle

## Otto Cycle Efficiency

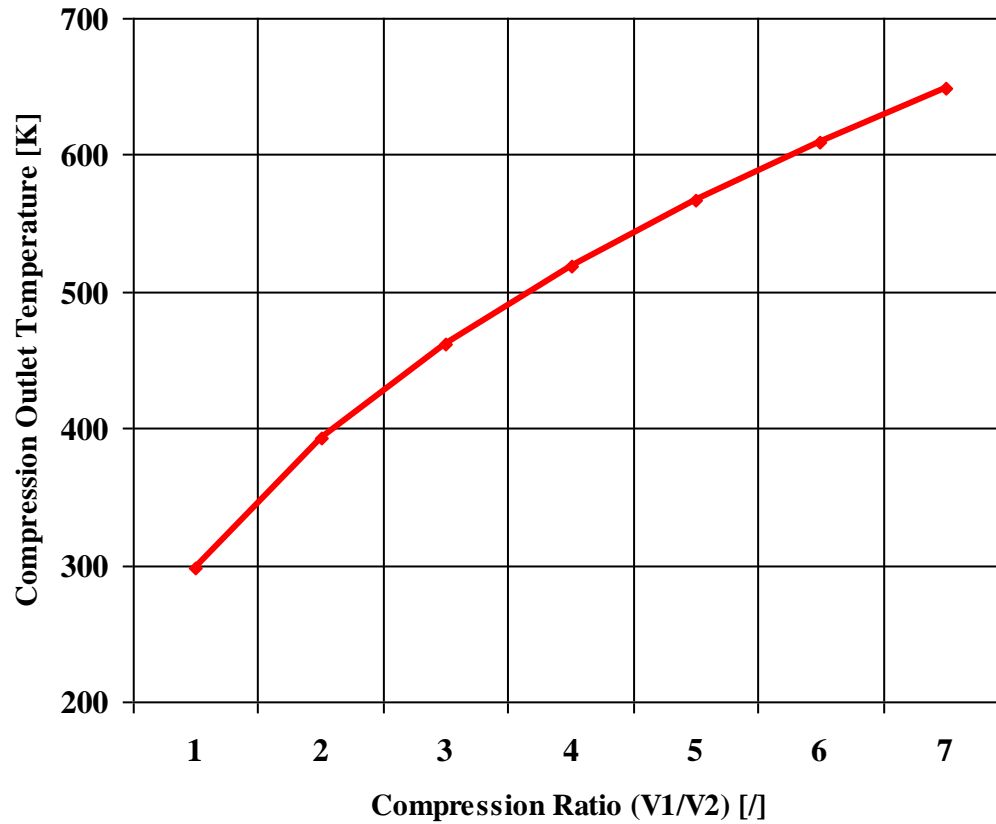


—◆—  $V_1/V_2$  [l]

Working Fluid: Air

# Otto Cycle

## Compression Outlet Temperature

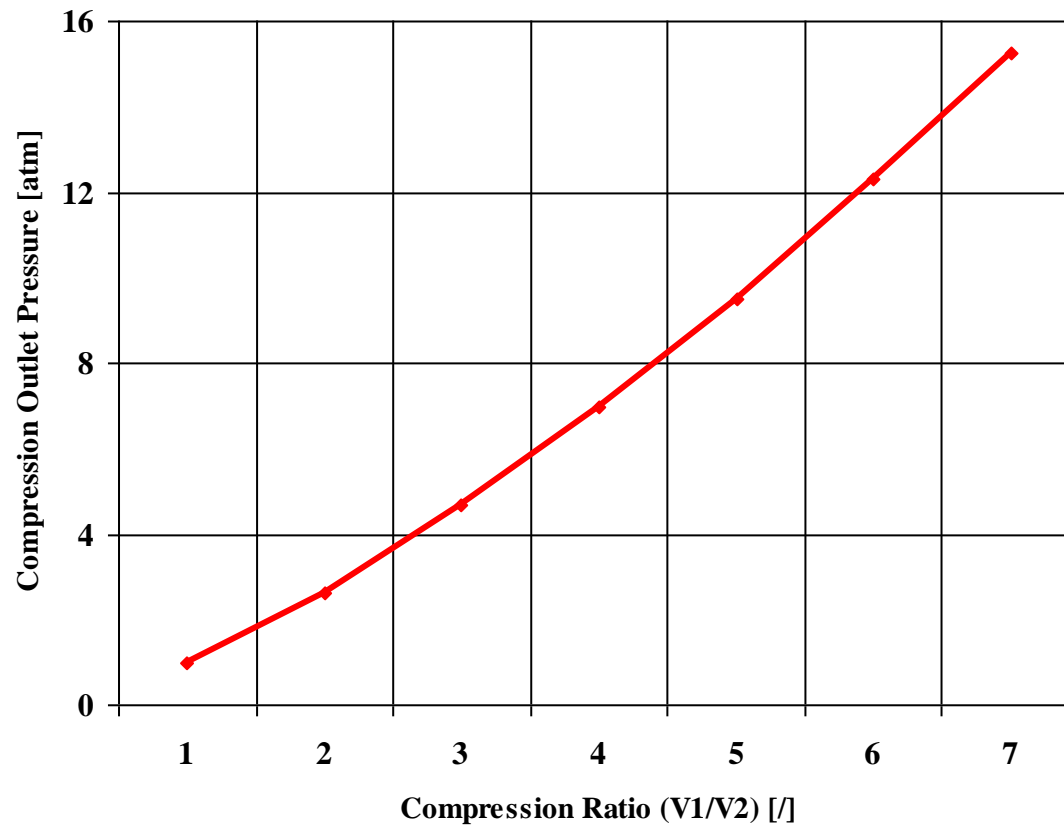


—◆— V1/V2 [ / ]

Working Fluid: Air

# Otto Cycle

## Compression Outlet Pressure

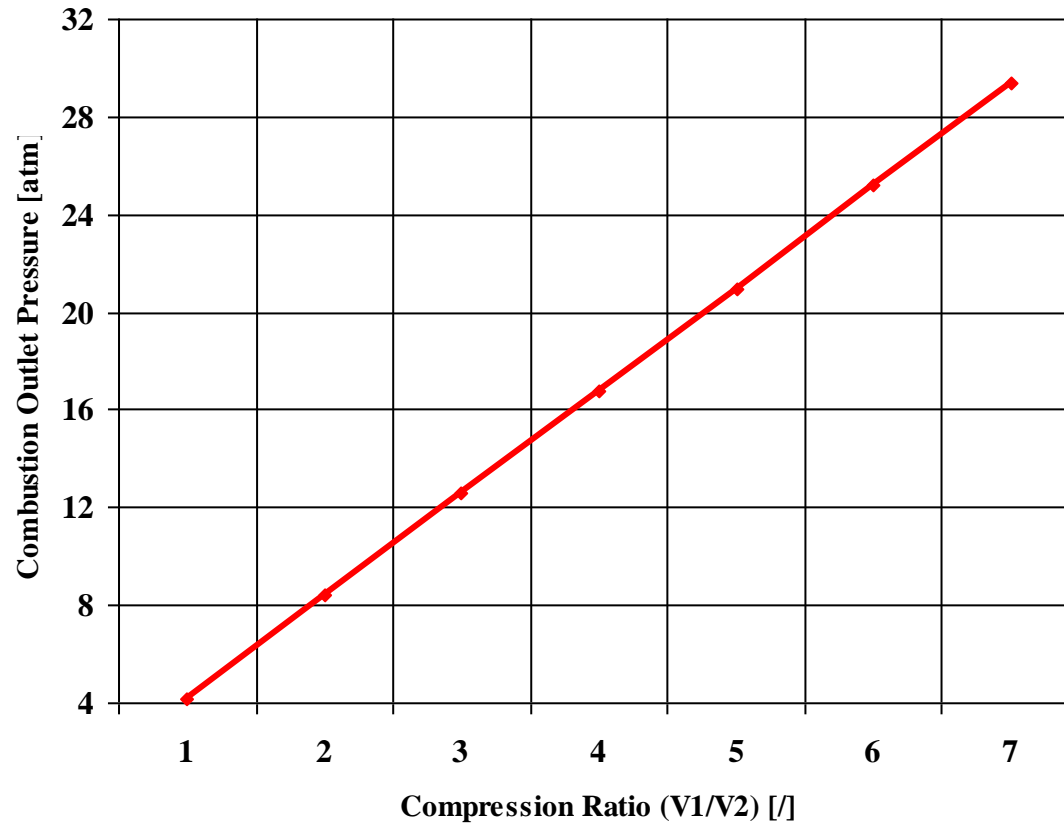


—●—  $V_1/V_2$  [ / ]

Working Fluid: Air

# Otto Cycle

## Combustion Outlet Pressure

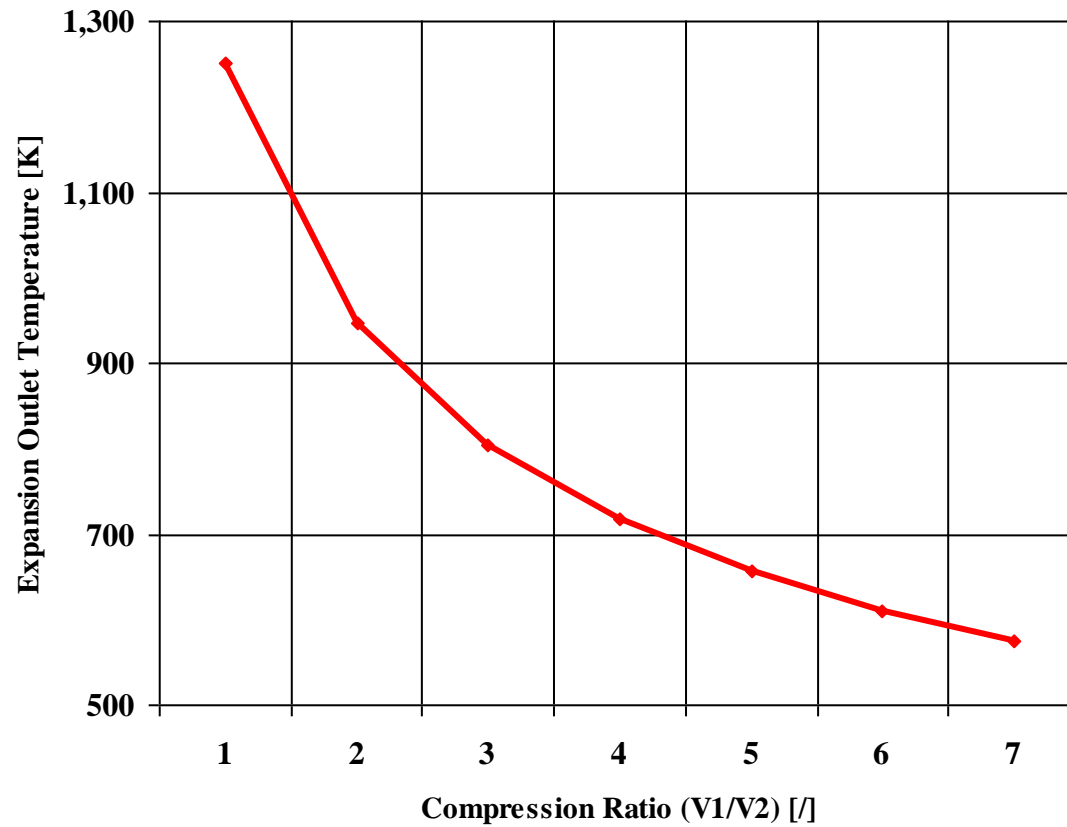


—◆—  $V_1/V_2$  [ / ]

Working Fluid: Air

# Otto Cycle

## Expansion Outlet Temperature

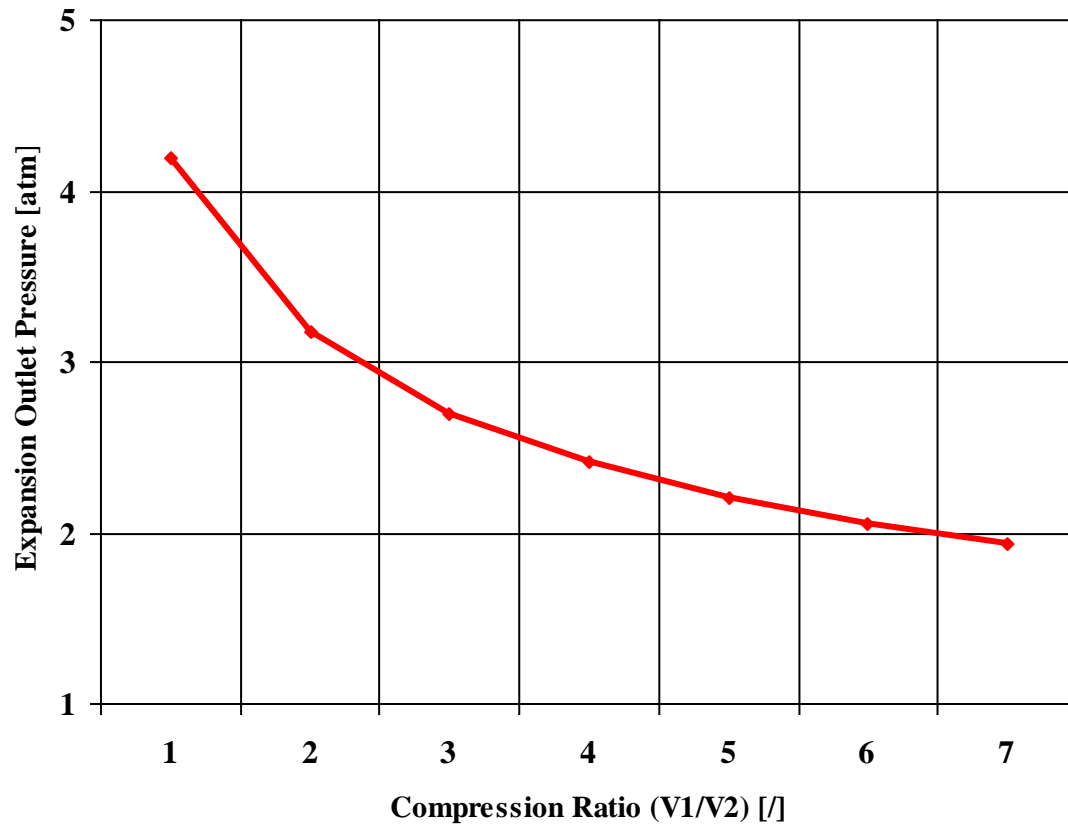


—◆— V1/V2 [ / ]

Working Fluid: Air

# Otto Cycle

## Expansion Outlet Pressure



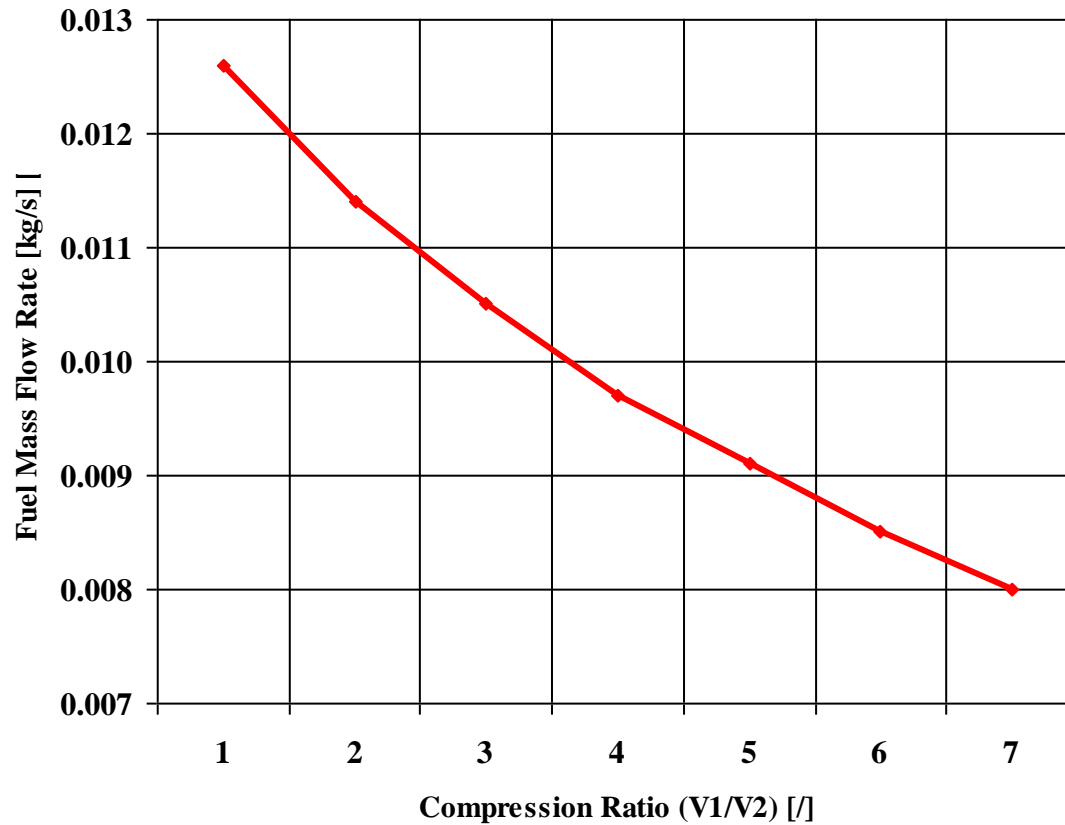
—◆—  $V_1/V_2$  [l]

Working Fluid: Air



# Otto Cycle

## Fuel Mass Flow Rate

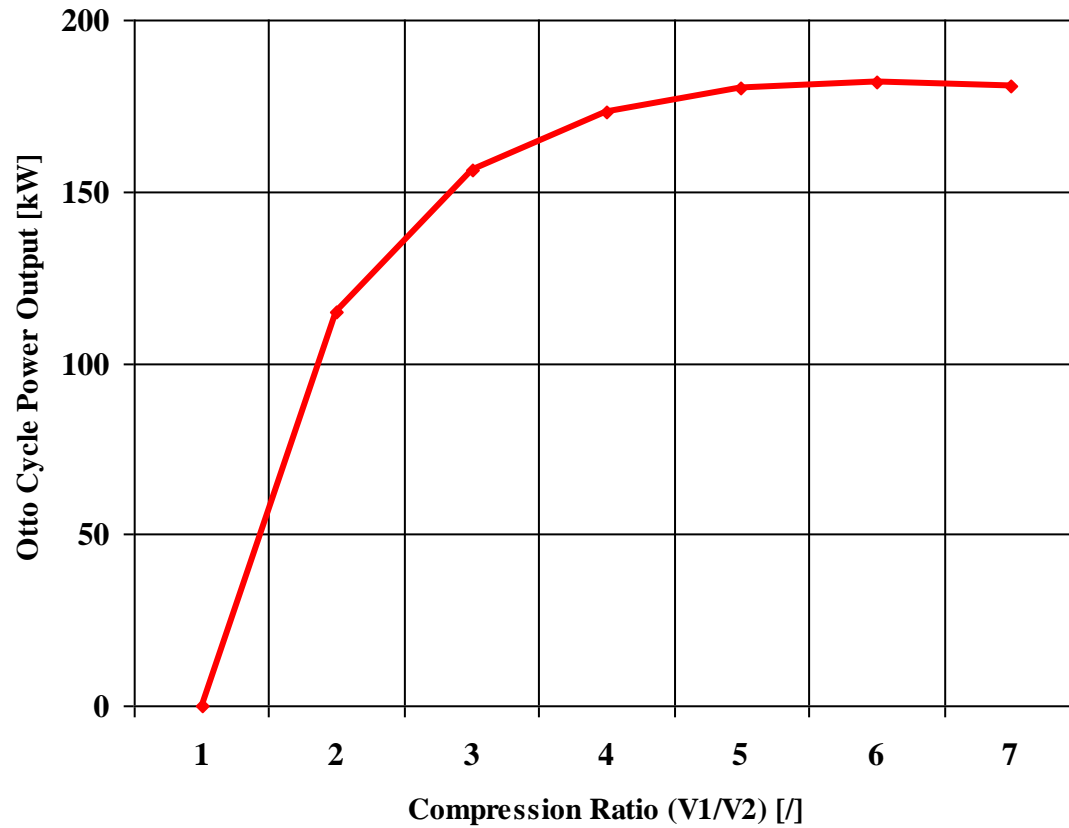


—◆—  $V_1/V_2$  [l]

Working Fluid: Air

# Otto Cycle

## Otto Cycle Power Output

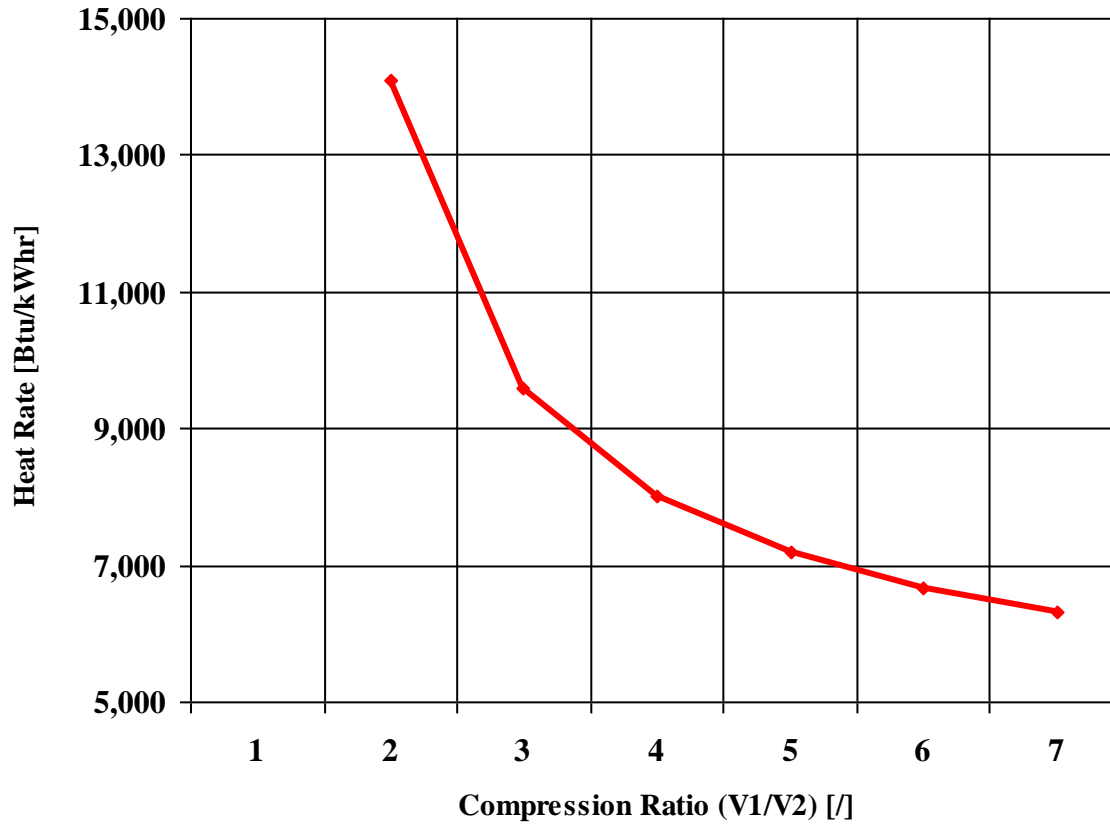


—●—  $V_1/V_2$  [r]

Working Fluid: Air

# Otto Cycle

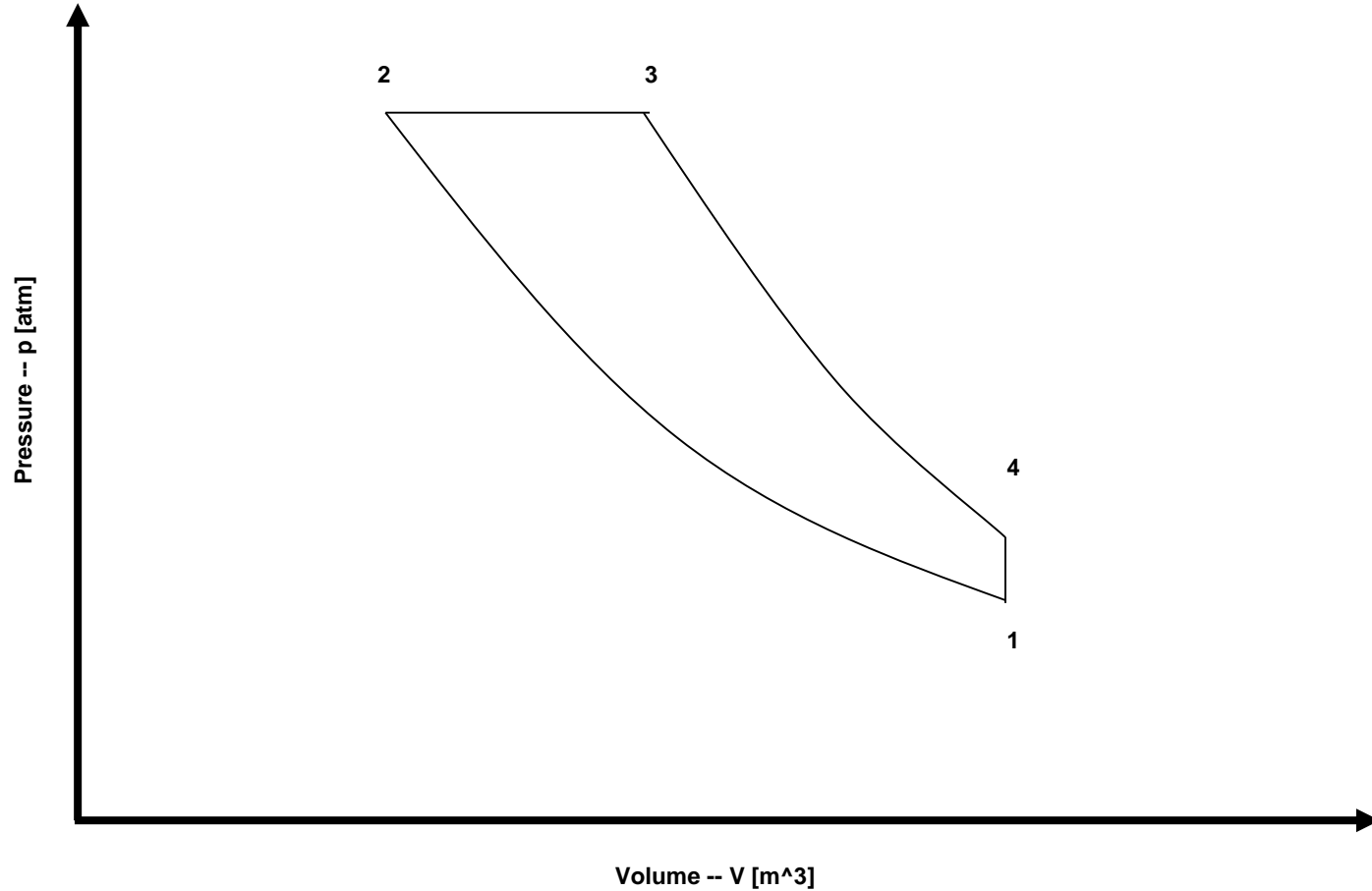
## Heat Rate



—◆— V1/V2 [/]

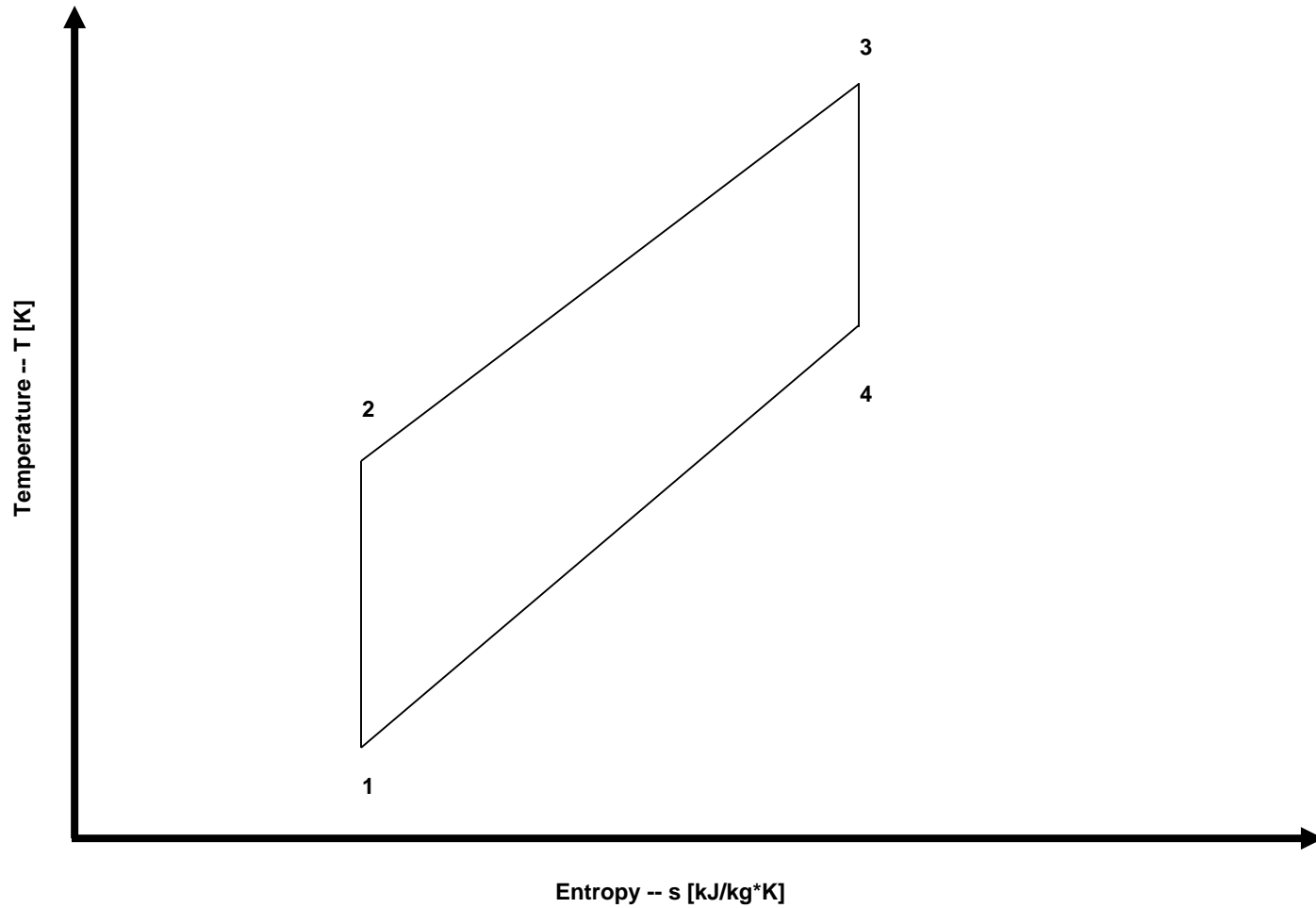
Working Fluid: Air

# Diesel Cycle



Diesel Cycle  $p$  -  $V$  Diagram

# Diesel Cycle



Diesel Cycle T - s Diagram

# Diesel Cycle

## Assumptions

Ambient Temperature: 298 [K]

Ambient Pressure: 1 [atm]

Compression Ratio: 15 [/]

Cut Off Ratio: 1.5 [/]

Working Fluid  $\gamma$  : 1.4 [/]

Working Fluid Gas Constant: 0.2867 [kJ/kg\*K]

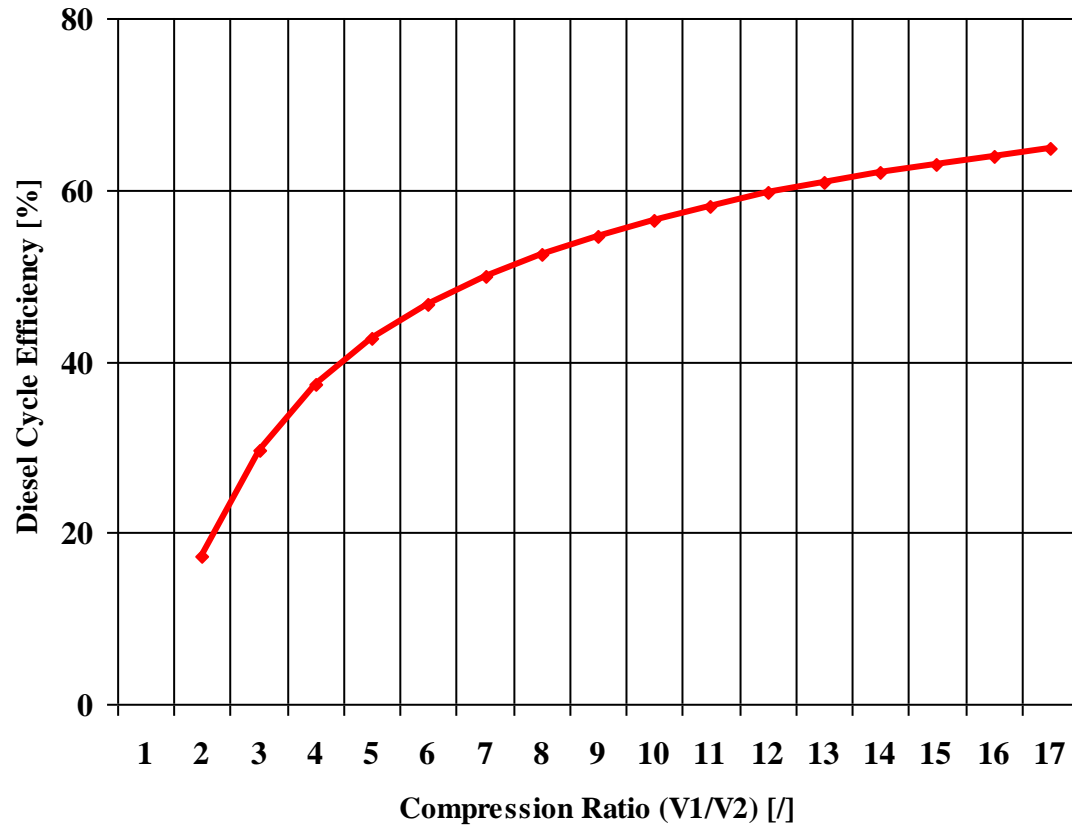
Working Fluid Specific Heat: 1.004 [kJ/kg\*K]

Working Fluid Mass Flow Rate: 0.78 [kg/s]

Fuel HHV: 18,000 [Btu/lbm]

# Diesel Cycle

## Diesel Cycle Efficiency

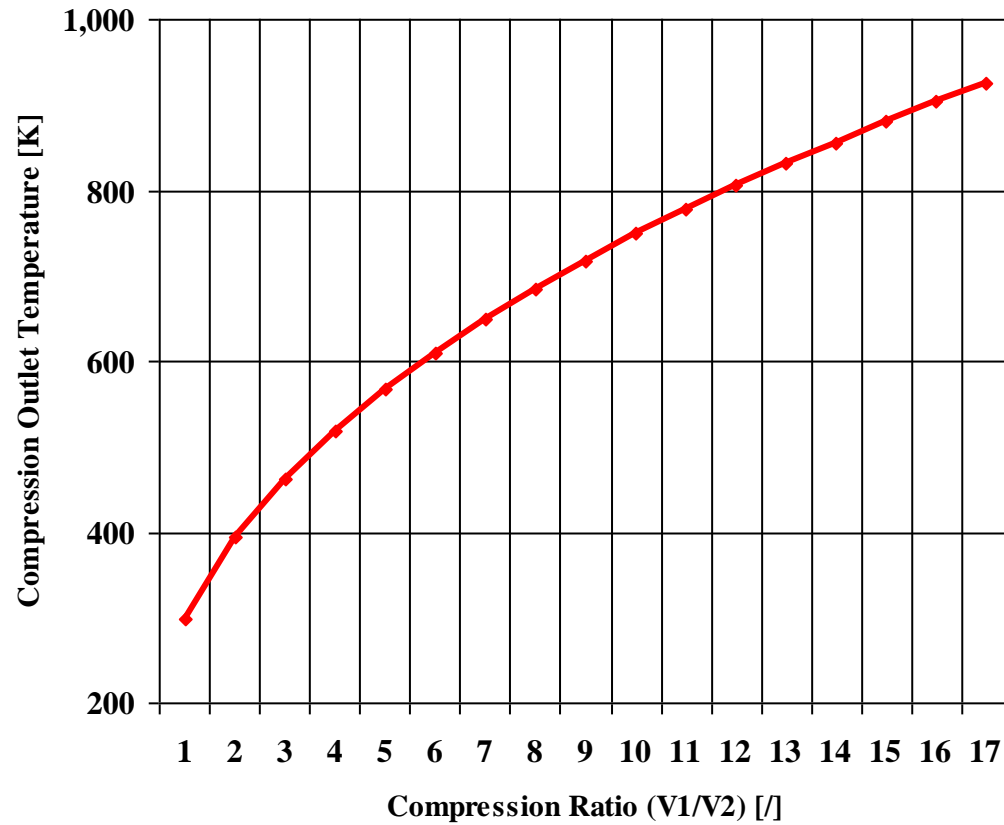


—◆—  $V_1/V_2$  [ / ]

Working Fluid: Air

# Diesel Cycle

## Compression Outlet Temperature



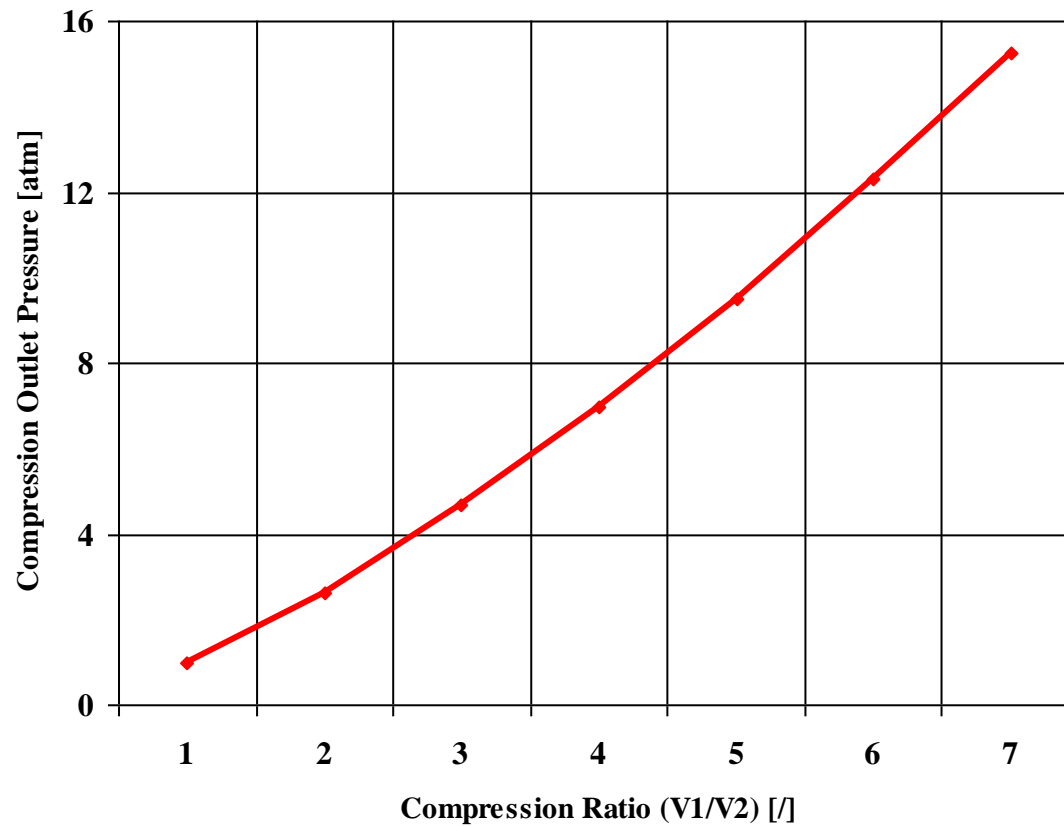
—◆—  $V_1/V_2$  [ / ]

Working Fluid: Air



# Diesel Cycle

## Compression Outlet Pressure

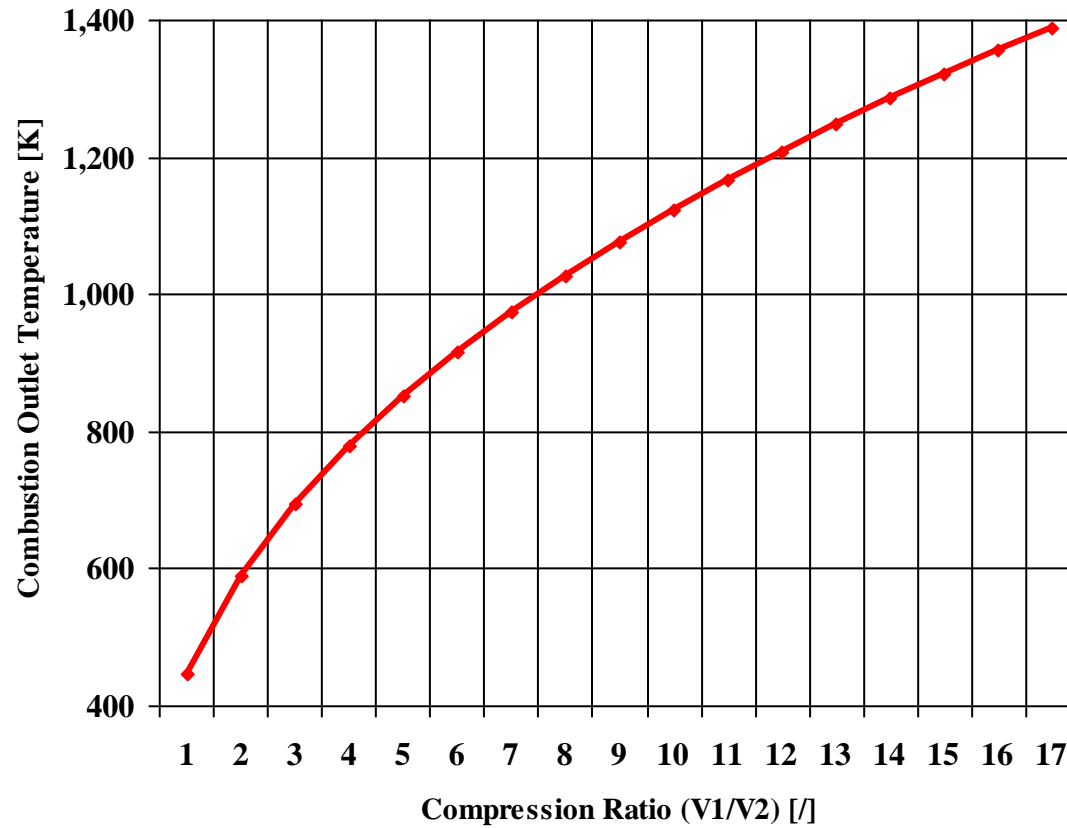


—◆—  $V_1/V_2$  [ / ]

Working Fluid: Air

# Diesel Cycle

## Combustion Outlet Temperature

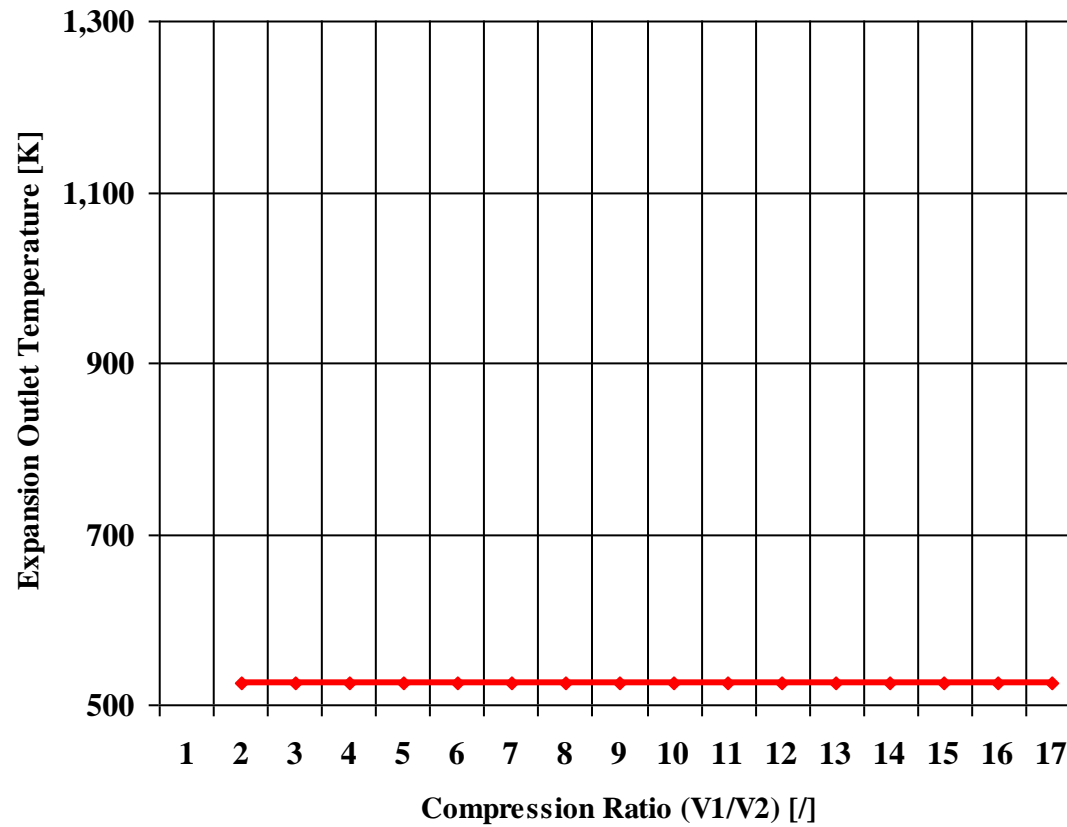


—◆—  $V_1/V_2$  [ / ]

Working Fluid: Air

# Diesel Cycle

## Expansion Outlet Temperature

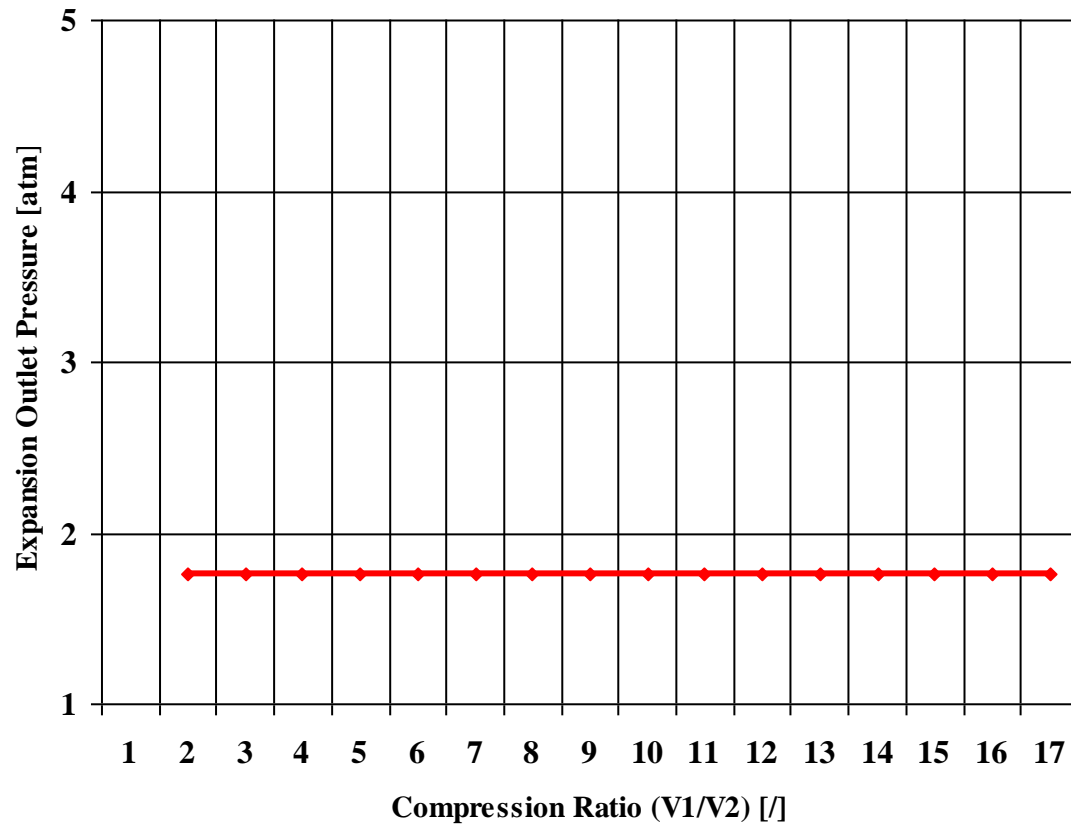


—◆—  $V_1/V_2$  [/]

Working Fluid: Air

# Diesel Cycle

## Expansion Outlet Pressure

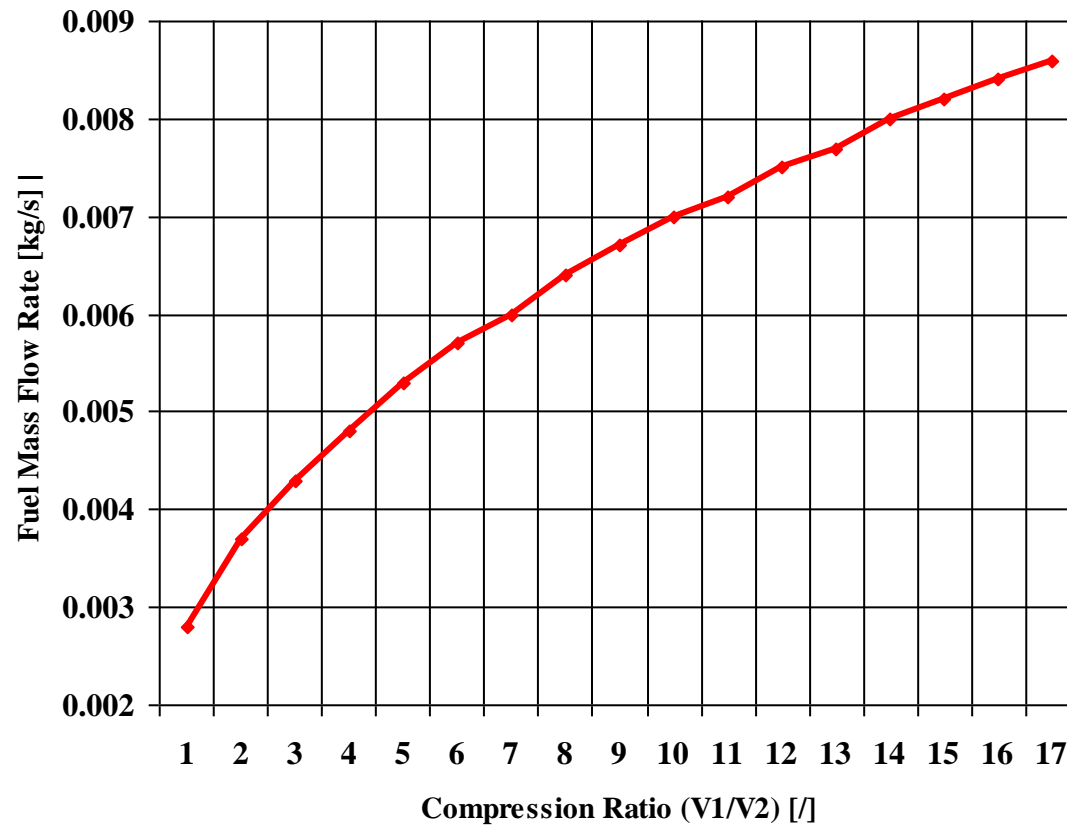


—◆—  $V_1/V_2$  [/]

Working Fluid: Air

# Diesel Cycle

## Fuel Mass Flow Rate

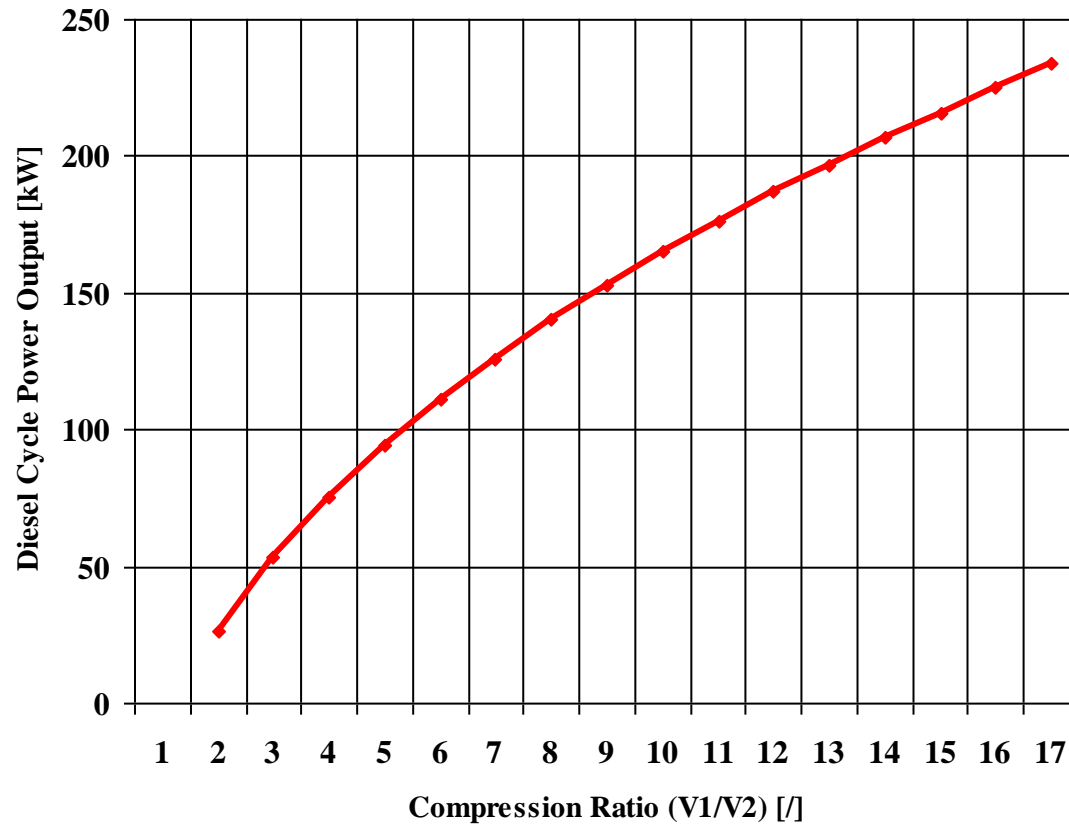


—◆—  $V_1/V_2$  [ ]

Working Fluid: Air

# Diesel Cycle

## Diesel Cycle Power Output

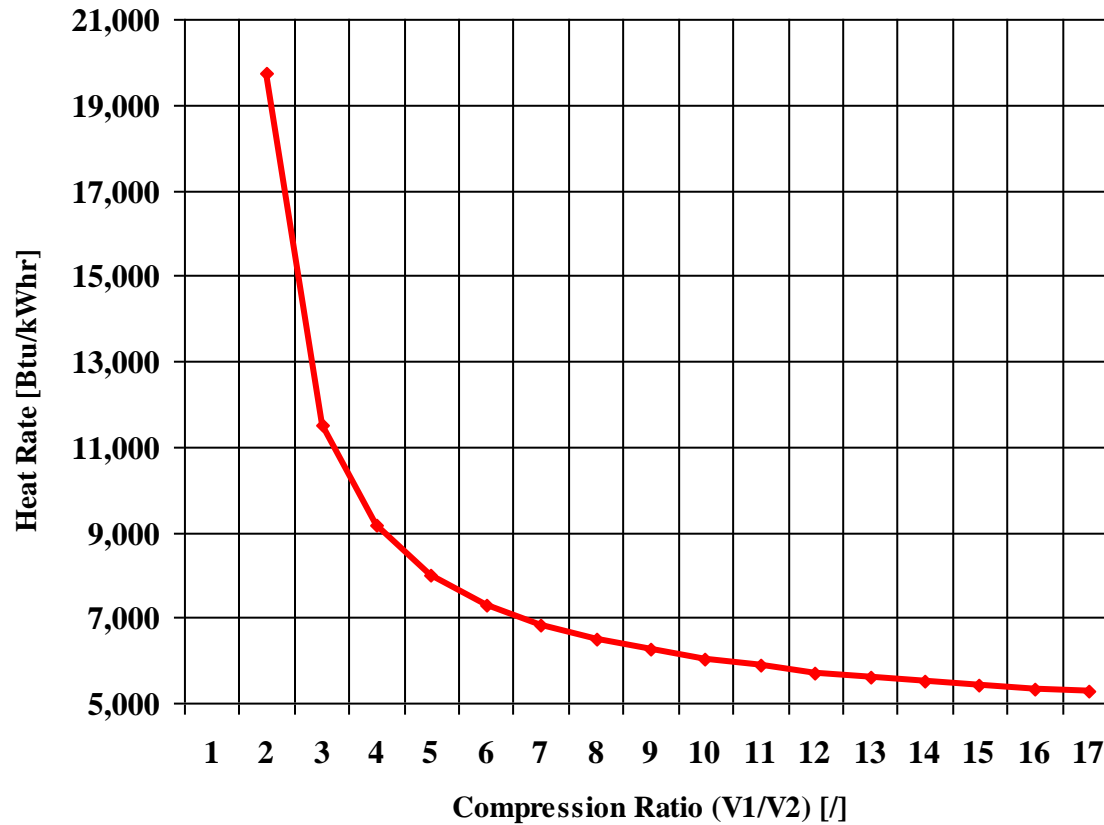


—◆—  $V_1/V_2$  [l]

Working Fluid: Air

# Diesel Cycle

## Heat Rate



—◆— V1/V2 [l]

Working Fluid: Air

# Power Cycles Analysis Conclusions

The Carnot Cycle efficiency increases with an increase in the heat addition temperature when the heat rejection temperature does not change at all. Furthermore, the Carnot Cycle efficiency decreases with an increase in the heat rejection temperature when the heat addition temperature does not change at all.

The Carnot Cycle efficiency is not dependent on the working fluid properties.

The Brayton Cycle specific power output increases with an increase in the gas turbine inlet temperature. Furthermore, the increase is greater for the higher compression ratio. The Brayton Cycle power output increases with an increase in the working fluid mass flow rate. The increase is greater for the higher compression ratio values.

The Otto Cycle efficiency increases with an increase in the compression ratio. Also, the Otto Cycle power output increases with an increase in the combustion temperature and the Otto Cycle power output is greater for higher compression ratio values.

The Diesel Cycle efficiency increases with an increase in the compression ratio and with a decrease in the cut off ratio values. Also, the Diesel Cycle power output increases with an increase in the compression ratio and the combustion temperature -- the Diesel Cycle power output is greater for lower cut off ratio values for given combustion temperature values.